

Spatial Data and Cartography (Part 2)

Lecture 17

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sf object summary

From last time,

- `sf` class is an extension of `data.frame` / `tibble` that includes a `geometry` column
- The geometry column is a list column with the `sfc` class
 - This column also tracks the CRS of the geometry (set via `st_crs()` or transformed by `st_transform()`)
- Elements of the geometry column are objects with the `sfg` class
 - S3 class also contains the simple feature geometry type and coordinate type

Plotting

Example Data - NC SIDS

```
1 ( nc = read_sf(system.file("shape/nc.shp", package="sf"), quiet = TRUE) |>
2   select(-(AREA:CNTY_ID), -(FIPS:CRESS_ID)))
```

Simple feature collection with 100 features and 7 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965

Geodetic CRS: NAD27

A tibble: 100 × 8

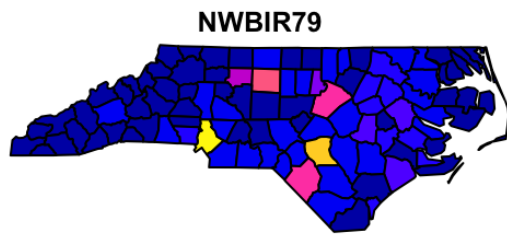
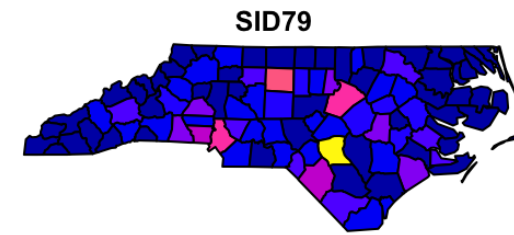
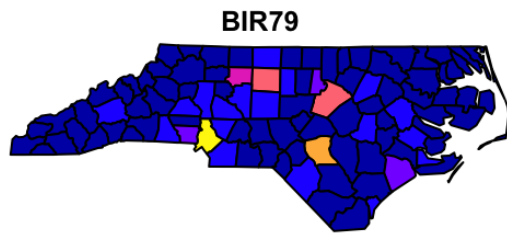
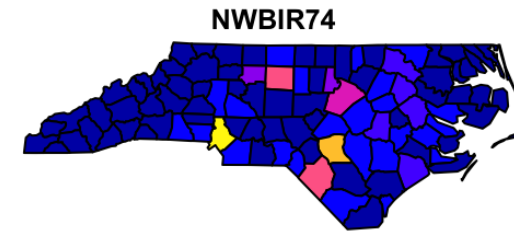
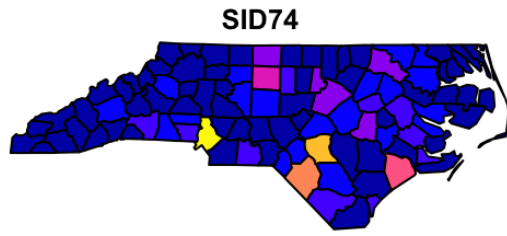
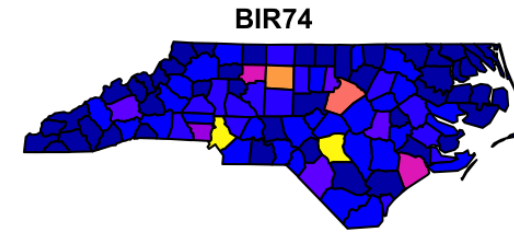
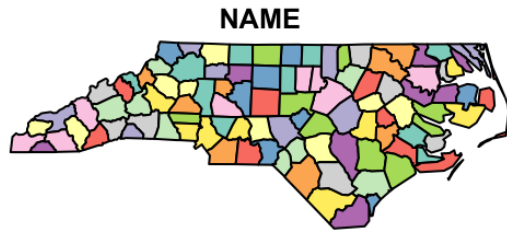
	NAME	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	Ashe	1091	1	10	1364	0	19
2	Alleghany	487	0	10	542	3	12
3	Surry	3188	5	208	3616	6	260
4	Currituck	508	1	123	830	2	145
5	Northampton	1421	9	1066	1606	3	1197
6	Hertford	1452	7	954	1838	5	1237
7	Camden	286	0	115	350	2	139
8	Gates	420	0	254	594	2	371
9	Warren	968	4	748	1190	2	844
10	Stokes	1612	1	160	2038	5	176

i 90 more rows

i 1 more variable: geometry <MULTIPOLYGON [°]>

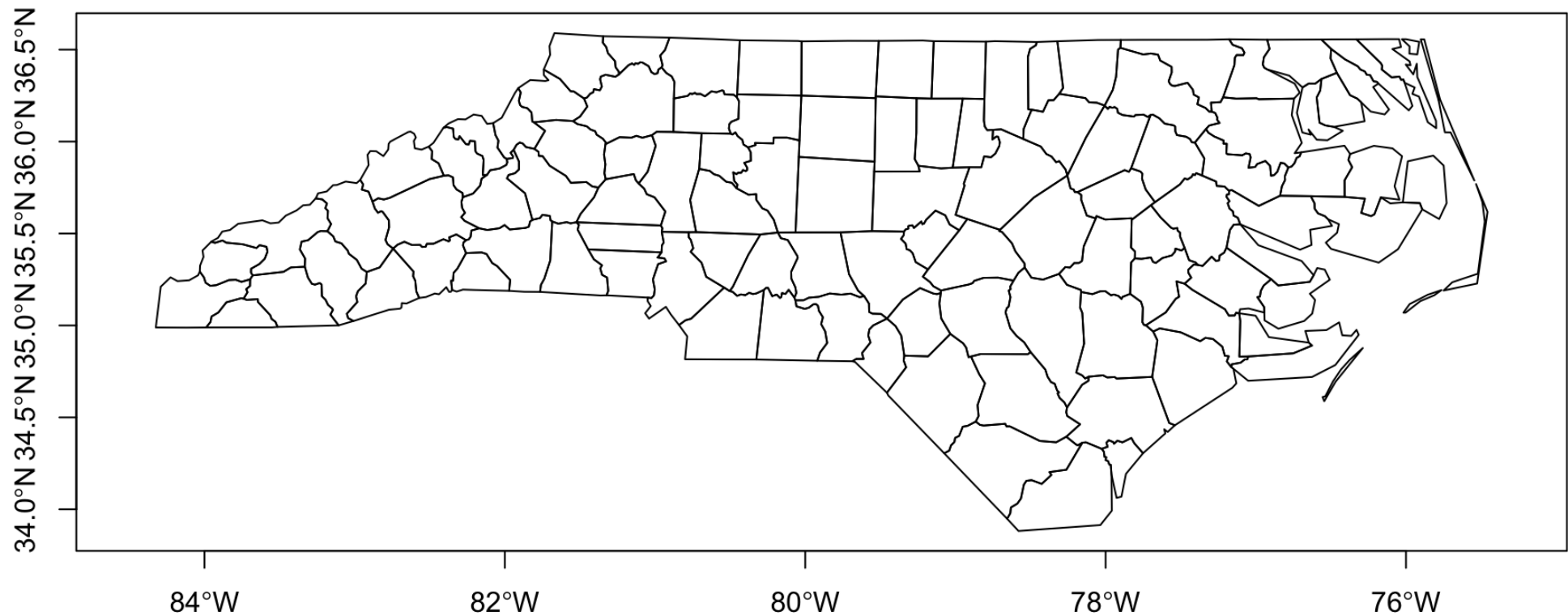
Base Plots

```
1 plot(nc)
```



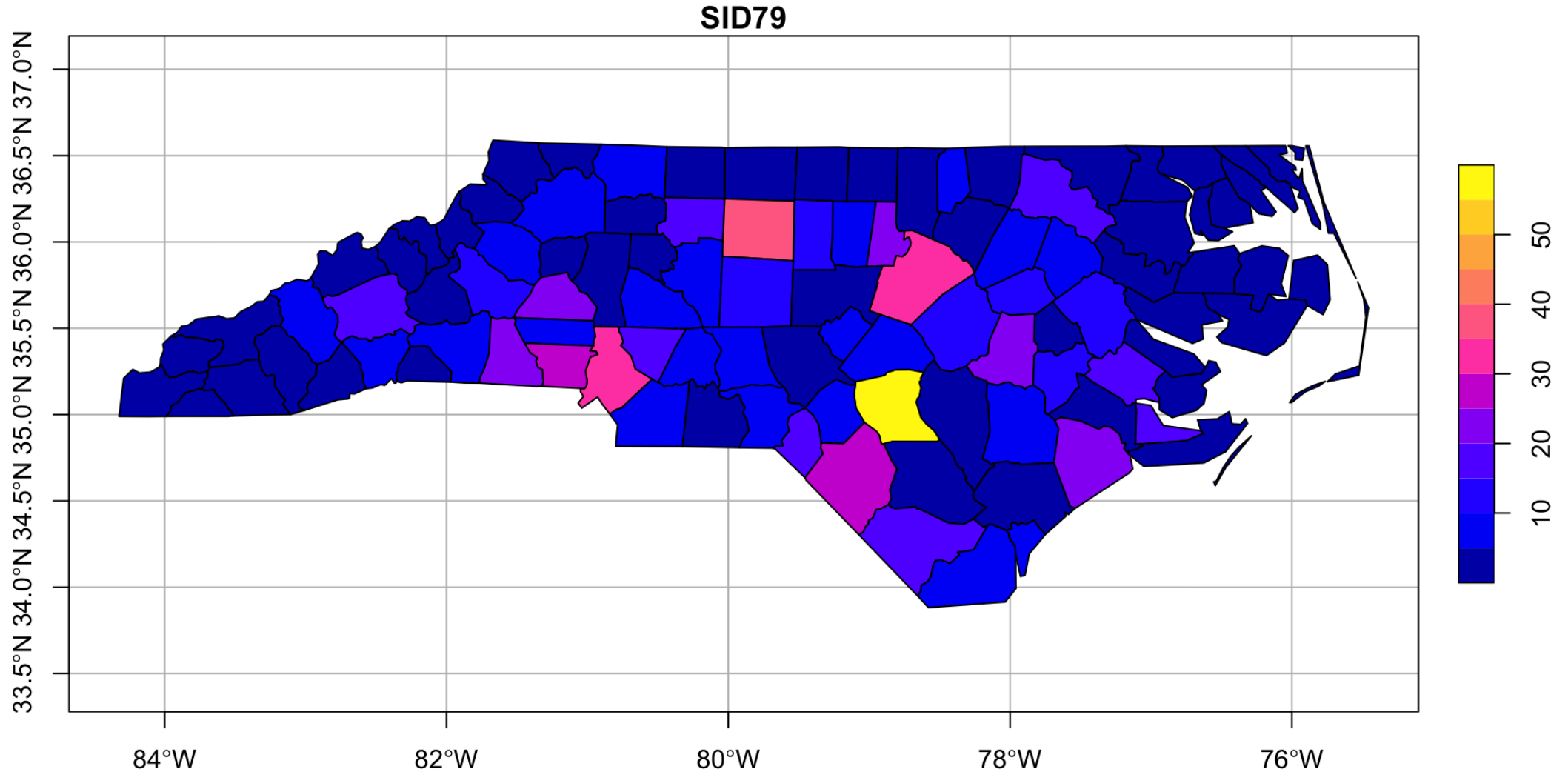
Geometry Plot

```
1 plot(st_geometry(nc), axes=TRUE)
```



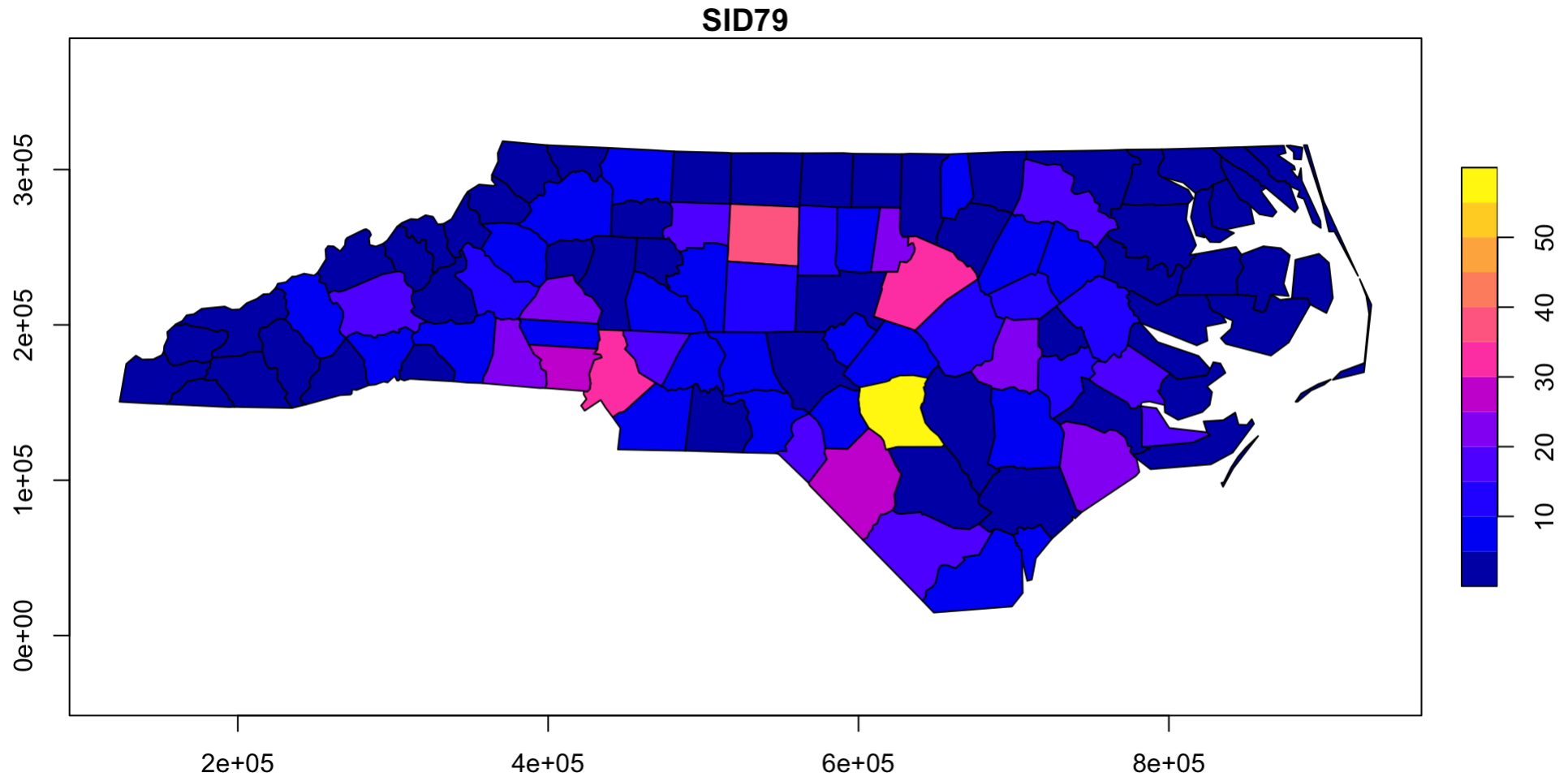
Graticules

```
1 plot(nc[, "SID79"], graticule=TRUE, axes=TRUE)
```



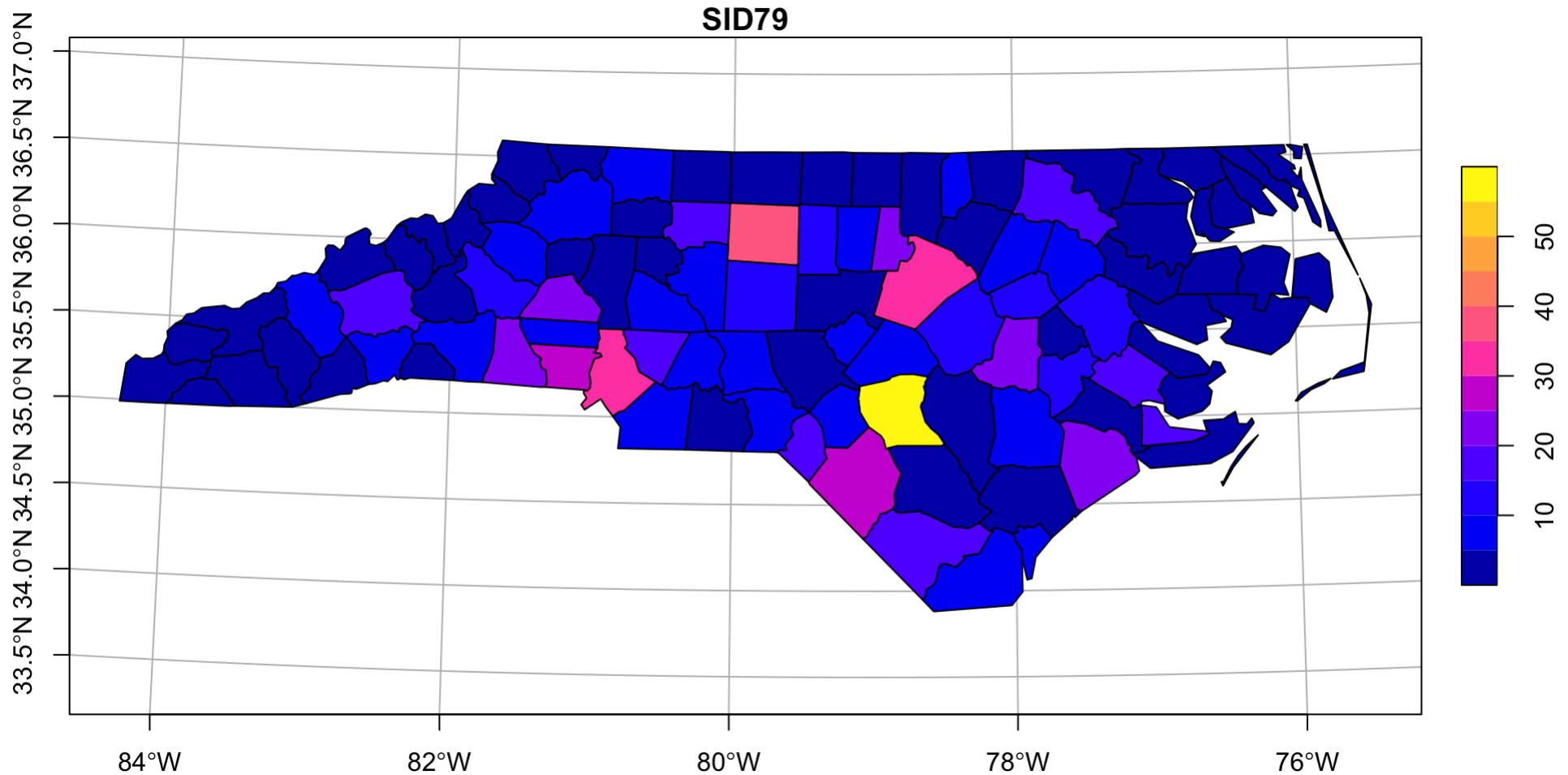
EPSG 3631

```
1 plot(st_transform(nc[, "SID79"], 3631), axes=TRUE)
```



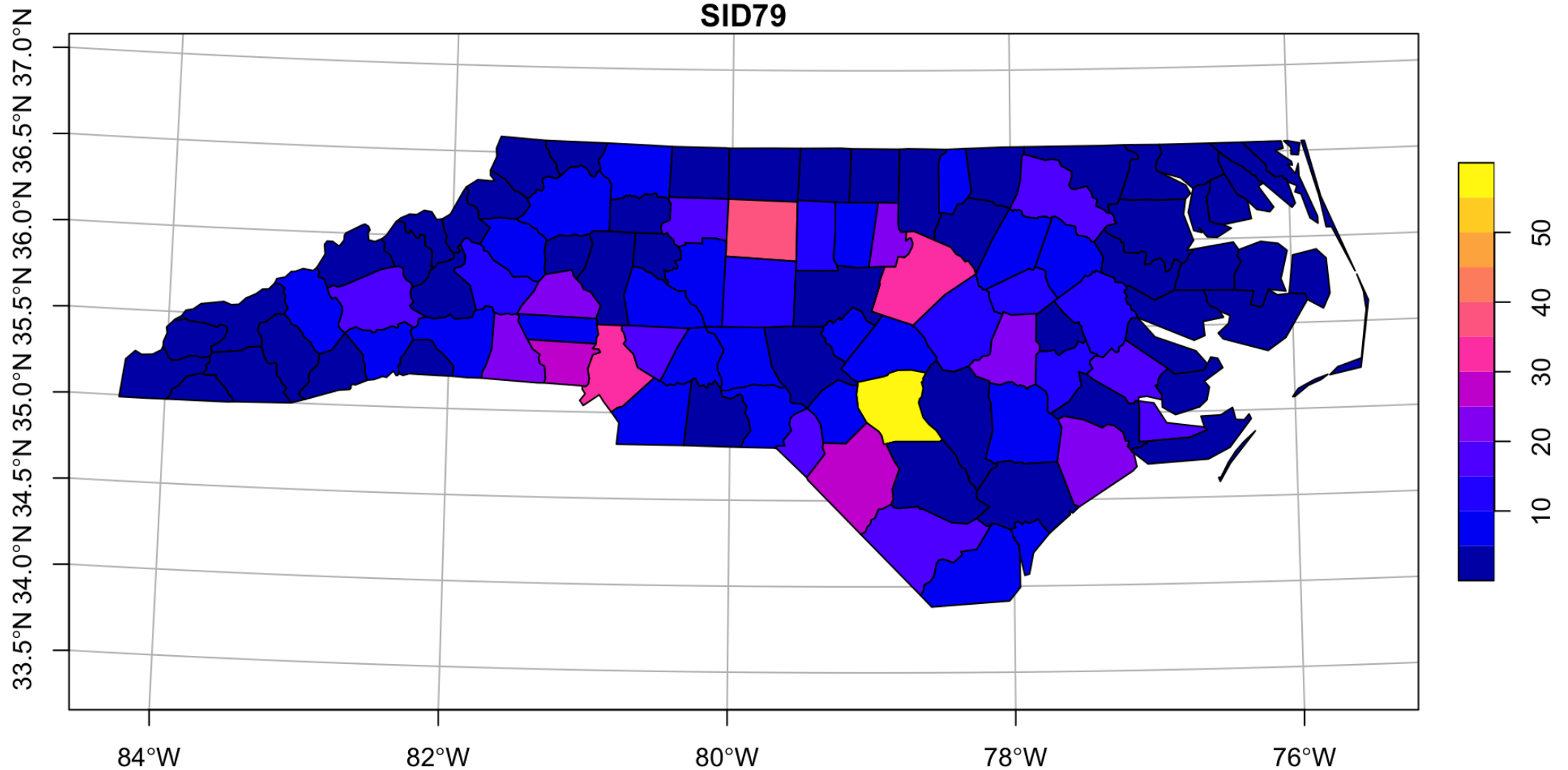
EPSG 3631 w/ Graticules

```
1 plot(st_transform(nc[, "SID79"], 3631), graticule=TRUE, axes=TRUE)
```



EPSG 3631 w/ Lat / long Graticules

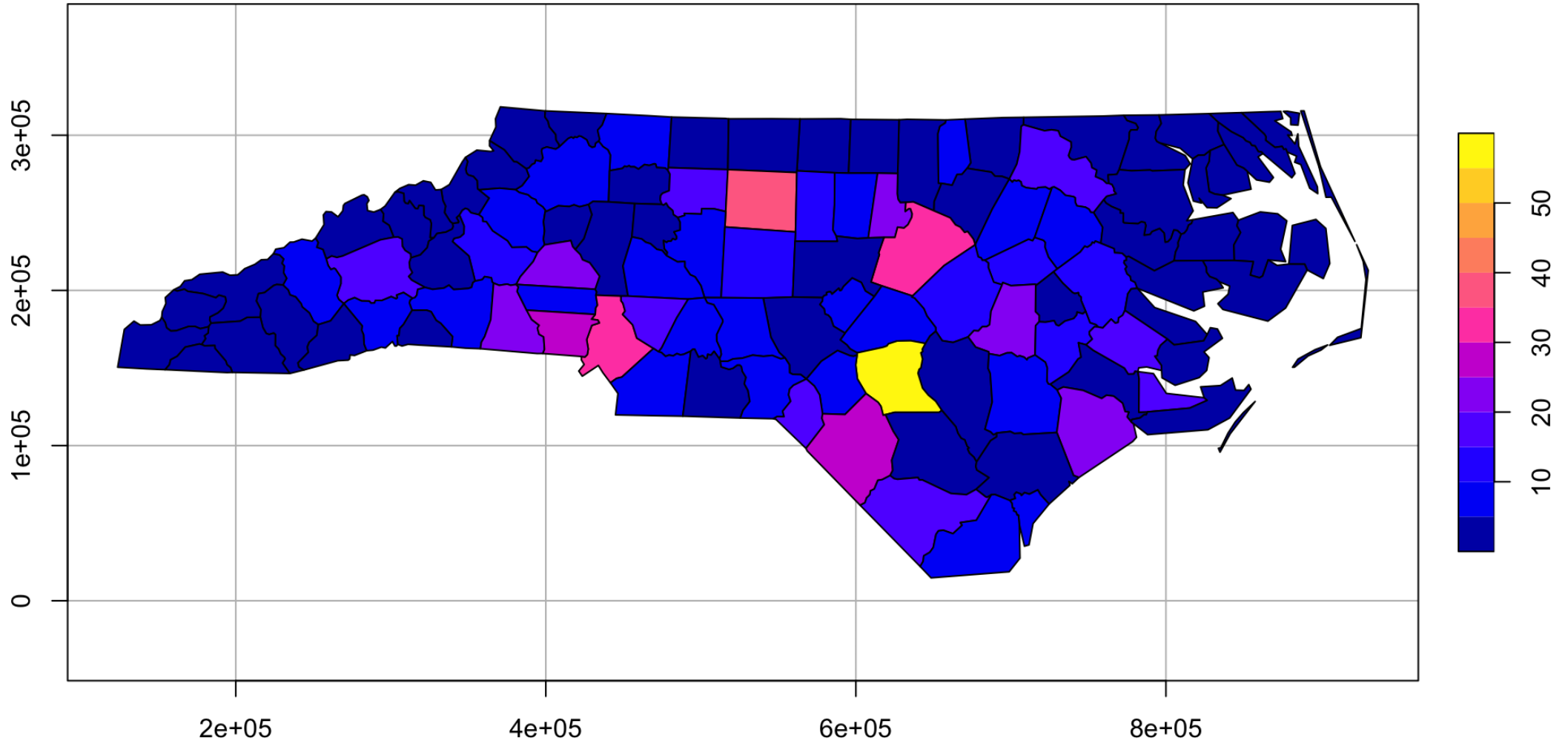
```
1 plot(st_transform(nc[, "SID79"], 3631), graticule=st_crs(4326), axes=TRUE)
```



EPSG 3631 w/ 3631 Graticules

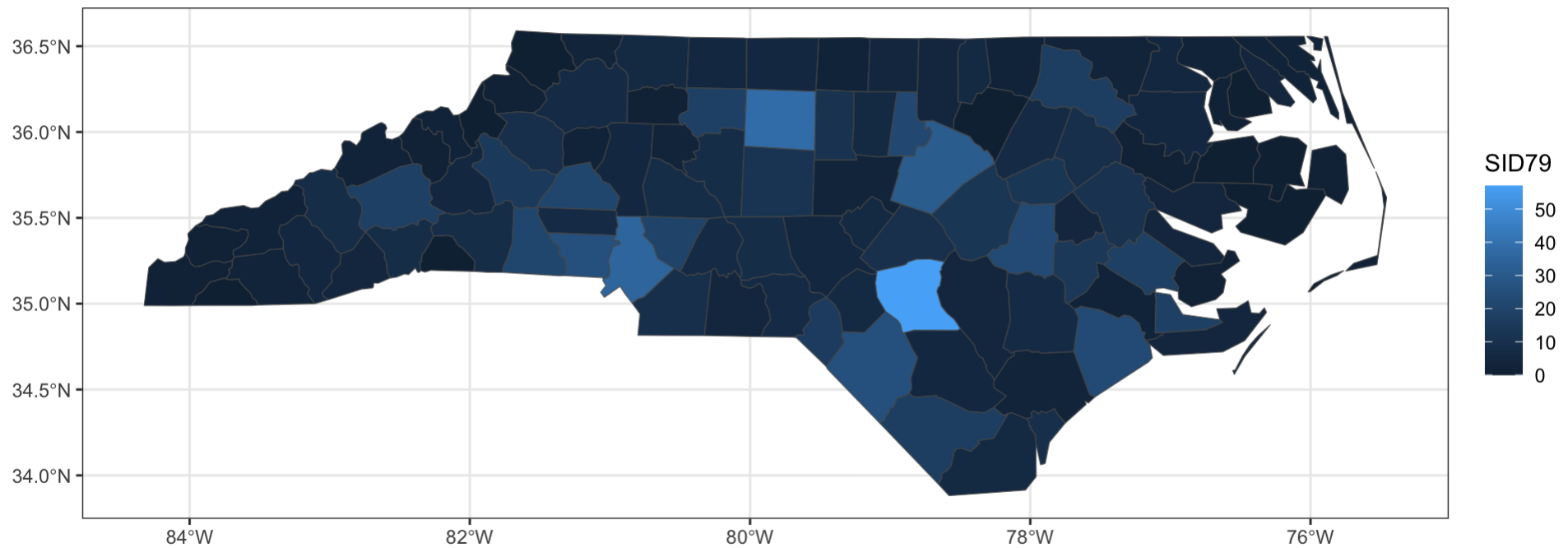
```
1 plot(st_transform(nc[, "SID79"], 3631), graticule=st_crs(3631), axes=TRUE)
```

SID79



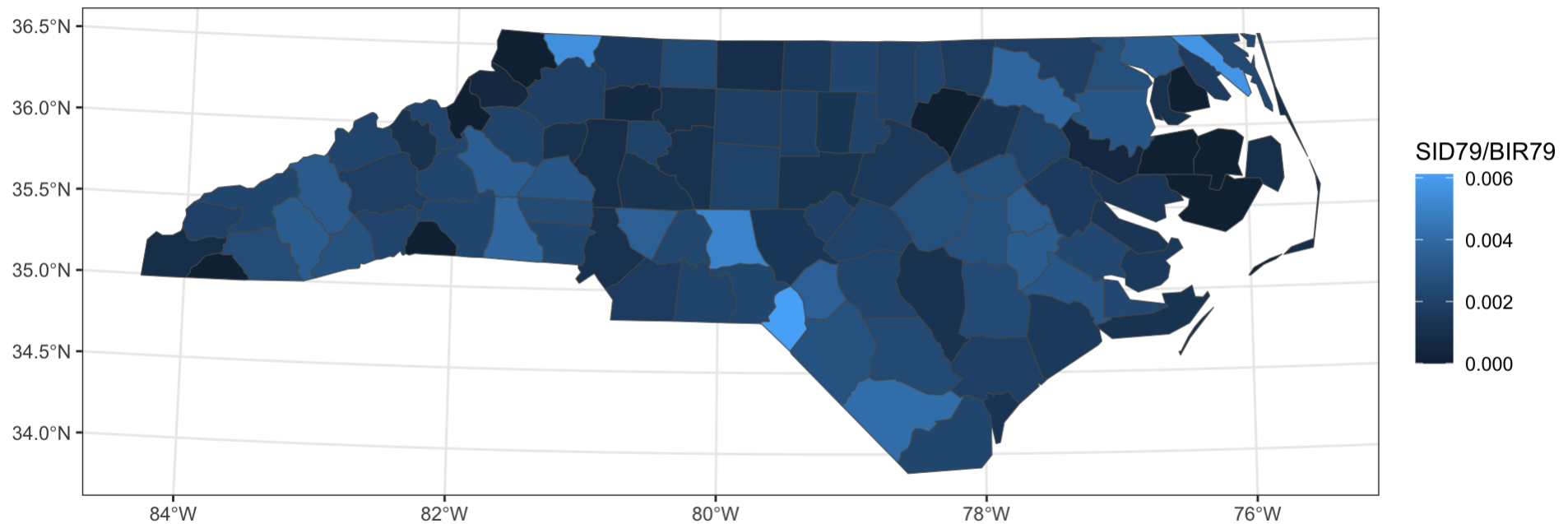
ggplot2

```
1 ggplot(nc) +  
2   geom_sf(aes(fill=SID79))
```



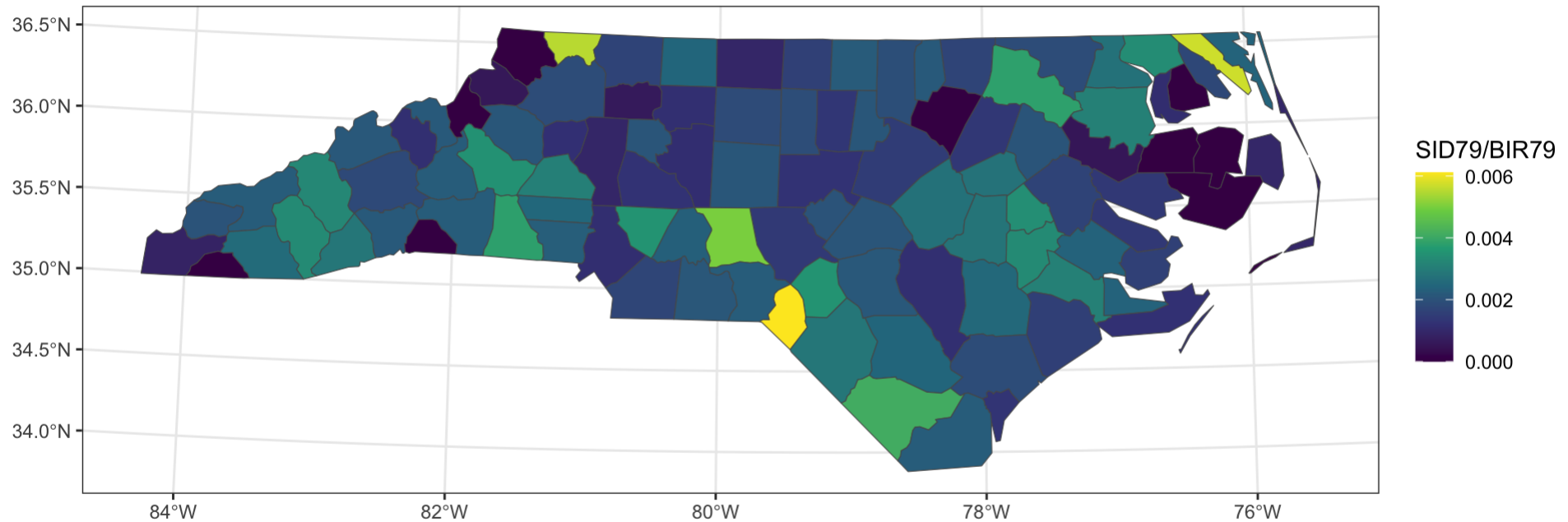
ggplot2 + projections

```
1 ggplot(st_transform(nc, 3631)) +  
2   geom_sf(aes(fill=SID79 / BIR79))
```



ggplot2 + viridis

```
1 ggplot(st_transform(nc, 3631)) +  
2   geom_sf(aes(fill=SID79 / BIR79)) +  
3   scale_fill_viridis_c()
```



Example Data - Meuse

```
1 data(meuse, meuse.riv, package="sp")
2 (meuse = st_as_sf(meuse, coords=c("x", "y"), crs=28992) |>
3   as_tibble() |> st_as_sf())
```

Simple feature collection with 155 features and 12 fields

Geometry type: POINT

Dimension: XY

Bounding box: xmin: 178605 ymin: 329714 xmax: 181390 ymax: 333611

Projected CRS: Amersfoort / RD New

A tibble: 155 × 13

	cadmium	copper	lead	zinc	elev	dist	om	ffreq	soil	lime	landuse	dist.m
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<fct>	<fct>	<fct>	<fct>	<dbl>
1	11.7	85	299	1022	7.91	0.00136	13.6	1	1	1	Ah	50
2	8.6	81	277	1141	6.98	0.0122	14	1	1	1	Ah	30
3	6.5	68	199	640	7.8	0.103	13	1	1	1	Ah	150
4	2.6	81	116	257	7.66	0.190	8	1	2	0	Ga	270
5	2.8	48	117	269	7.48	0.277	8.7	1	2	0	Ah	380
6	3	61	137	281	7.79	0.364	7.8	1	2	0	Ga	470
7	3.2	31	132	346	8.22	0.190	9.2	1	2	0	Ah	240
8	2.8	29	150	406	8.49	0.0922	9.5	1	1	0	Ab	120
9	2.4	37	133	347	8.67	0.185	10.6	1	1	0	Ab	240
10	1.6	24	80	183	9.05	0.310	6.3	1	2	0	W	420

i 145 more rows

i 1 more variable: geometry <POINT [m]>

```
1 ( meuse_riv = st_polygon(list(meuse.riv)) |>
2   st_sfc() |>
3   st_set_crs(28992) |>
4   st_as_sf()
5 )
```

Simple feature collection with 1 feature and 0 fields

Geometry type: POLYGON

Dimension: XY

Bounding box: xmin: 178304 ymin: 325698.5 xmax: 182331.5 ymax: 337684.8

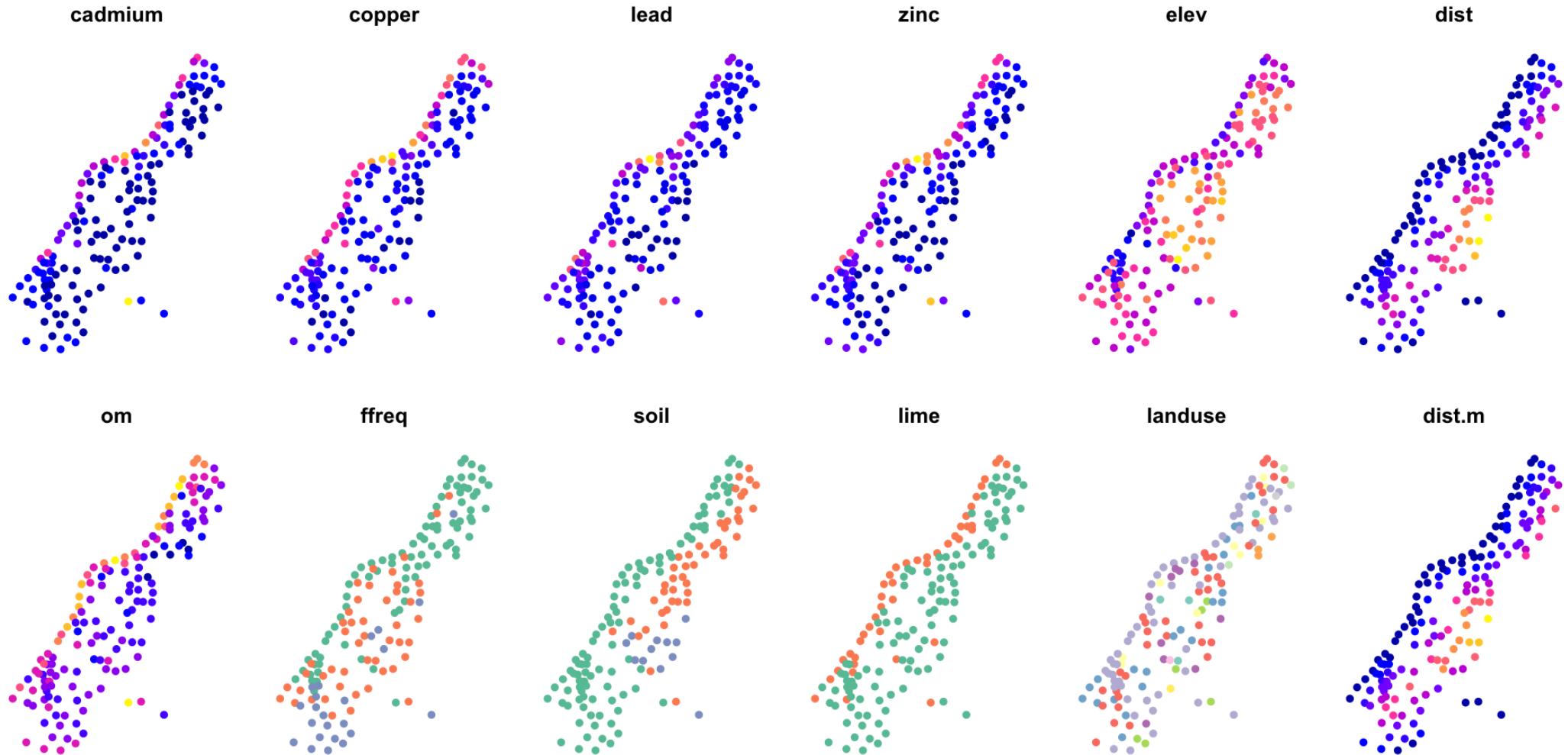
Projected CRS: Amersfoort / RD New

x

1 POLYGON ((182003.7 337678.6...

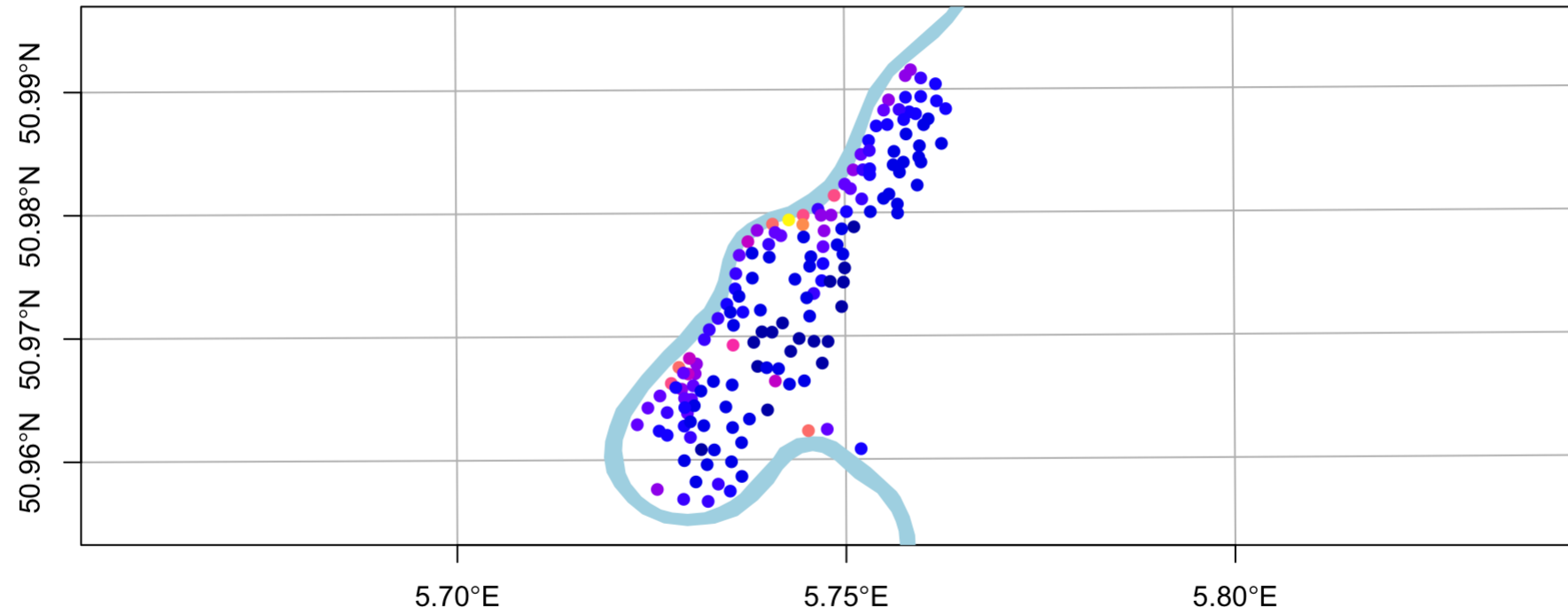
Meuse

```
1 plot(meuse, pch=16, max.plot=12)
```



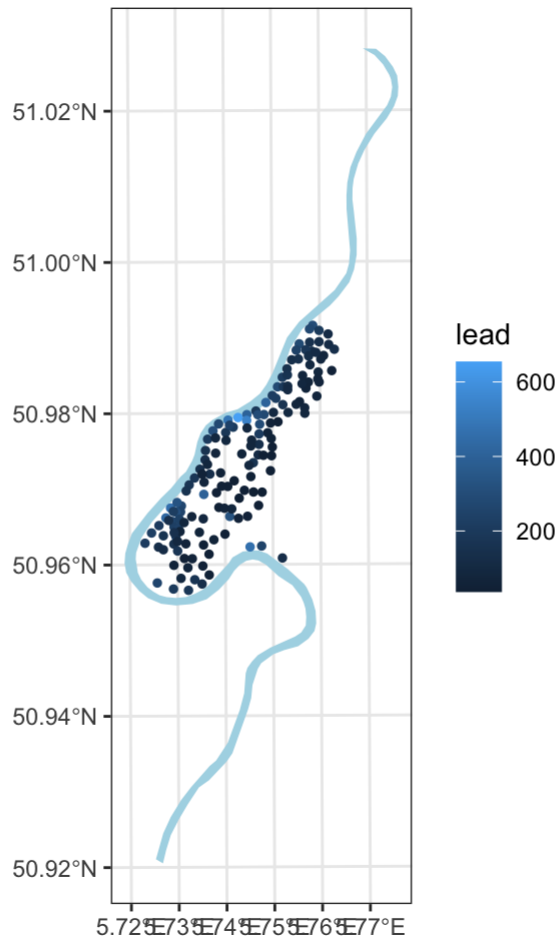
Layering plots

```
1 plot(  
2   meuse_riv, col=adjustcolor("lightblue", alpha.f=1), border = NA,  
3   axes=TRUE, graticule=st_crs(4326),  
4   ylim = c(329500, 334000)  
5 )  
6 plot(meuse[, "lead"], pch=16, add=TRUE)
```



ggplot2

```
1 ggplot() +  
2   geom_sf(data=meuse_riv, fill="lightblue", color=NA) +  
3   geom_sf(data=meuse, aes(color=lead), size=1)
```



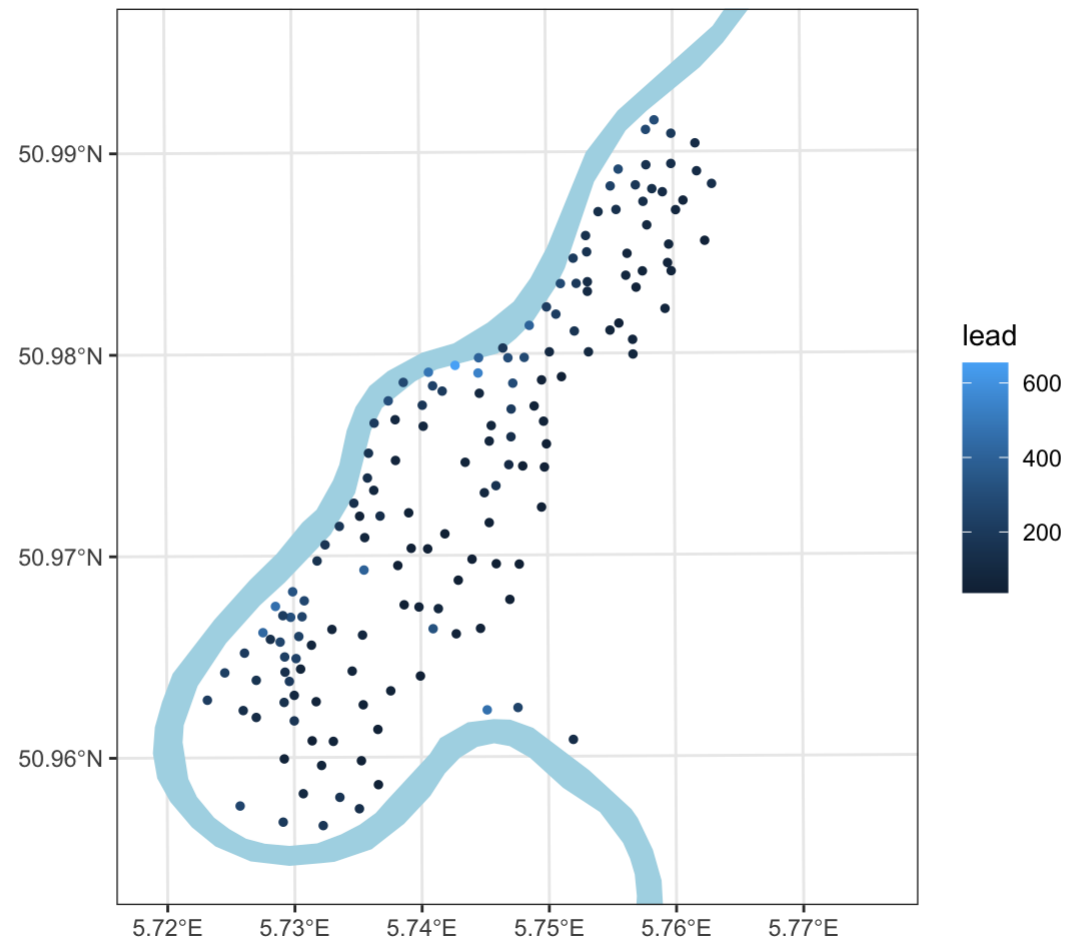
ggplot2 - axis limits

```
1 ggplot() +  
2   geom_sf(data=meuse_riv, fill="lightblue", color=NA) +  
3   geom_sf(data=meuse, aes(color=lead), size=1) +  
4   ylim(50.95, 50.99)
```



ggplot2 - axis limits

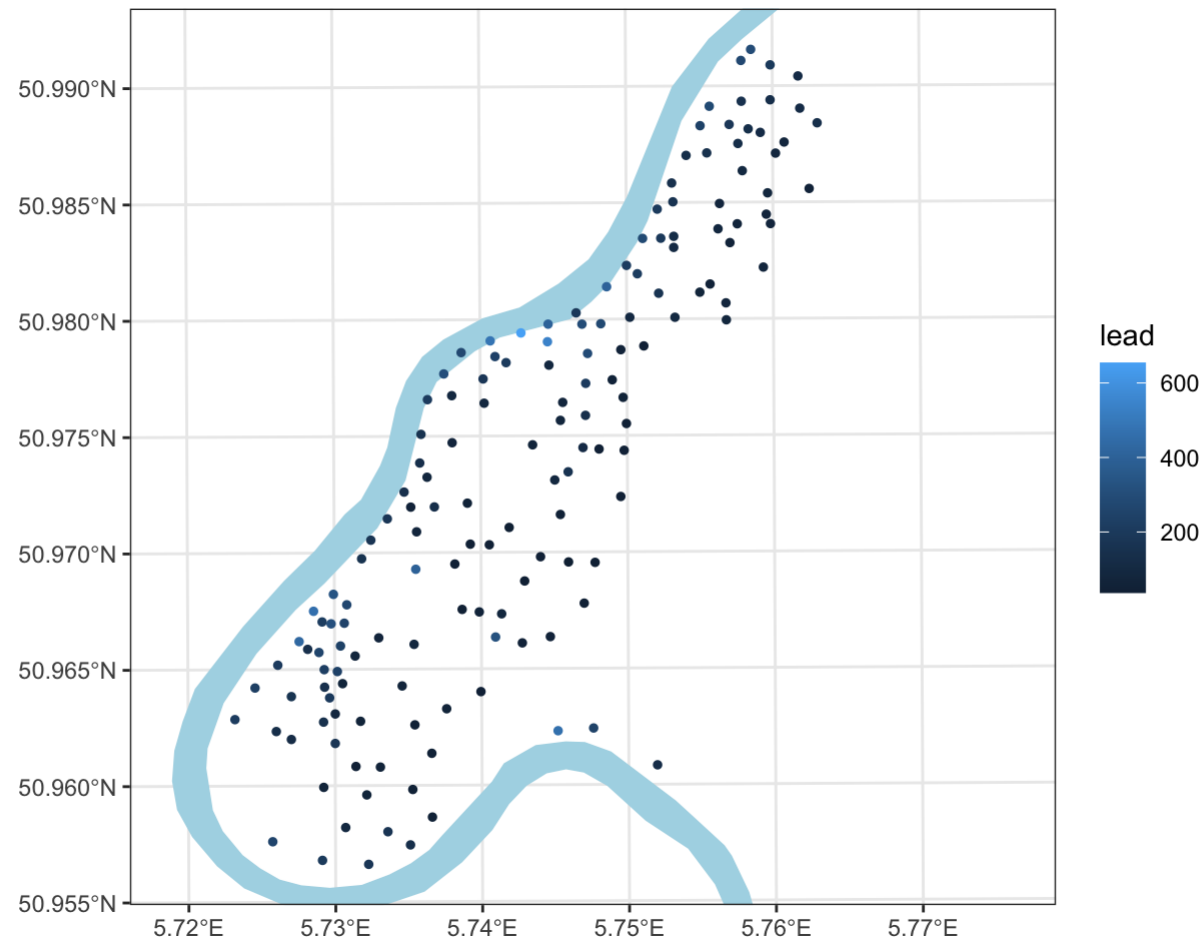
```
1 ggplot() +  
2   geom_sf(data=meuse_riv, fill="lightblue", color=NA) +  
3   geom_sf(data=meuse, aes(color=lead), size=1) +  
4   ylim(329500, 334000)
```



Sta 344/644 - Fall 2023

ggplot2 - bounding box

```
1 ggplot() +  
2   geom_sf(data=st_sf(meuse_riv), fill="lightblue", color=NA) +  
3   geom_sf(data=meuse, aes(color=lead), size=1) +  
4   ylim(st_bbox(meuse)["ymin"], st_bbox(meuse)["ymax"])
```



Geometry Predicates

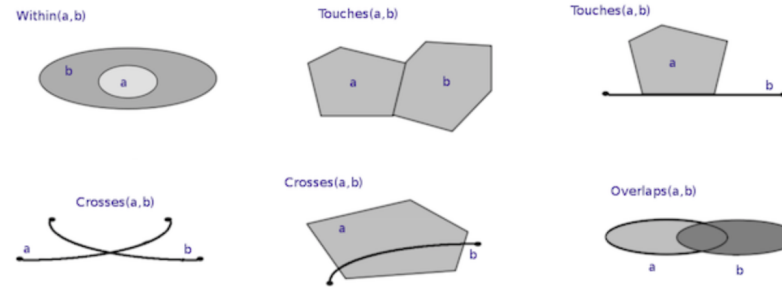
DE-9IM

a

b

	Interior	Boundary	Exterior
Interior	 $\dim[I(a) \cap I(b)] = 2$	 $\dim[I(a) \cap B(b)] = 1$	 $\dim[I(a) \cap E(b)] = 2$
Boundary	 $\dim[B(a) \cap I(b)] = 1$	 $\dim[B(a) \cap B(b)] = 0$	 $\dim[B(a) \cap E(b)] = 1$
Exterior	 $\dim[E(a) \cap I(b)] = 2$	 $\dim[E(a) \cap B(b)] = 1$	 $\dim[E(a) \cap E(b)] = 2$

Spatial predicates



`st_within(a,b):`

$$\begin{bmatrix} T & * & F \\ * & * & F \\ * & * & * \end{bmatrix}$$

`st_touches(a,b):`

$$\begin{bmatrix} F & T & * \\ * & * & * \\ * & * & * \end{bmatrix} \cup \begin{bmatrix} F & * & * \\ T & * & * \\ * & * & * \end{bmatrix} \cup \begin{bmatrix} F & * & * \\ * & T & * \\ * & * & * \end{bmatrix}$$

Sparse vs Full Results

```
1 st_intersects(ncc[20:30,], air) %>% str()
```

List of 11

```
$ : int(0)
$ : int(0)
$ : int(0)
$ : int(0)
$ : int(0)
$ : int 268
$ : int 717
$ : int(0)
$ : int(0)
$ : int(0)
$ : int(0)
- attr(*, "predicate")= chr "intersects"
- attr(*, "region.id")= chr [1:11] "1" "2" "3" "4" ...
- attr(*, "remove_self")= logi FALSE
- attr(*, "retain_unique")= logi FALSE
- attr(*, "ncol")= int 940
- attr(*, "class")= chr [1:2] "sgbp" "list"
```

```
1 st_intersects(ncc, air, sparse=FALSE) %>% str()
```

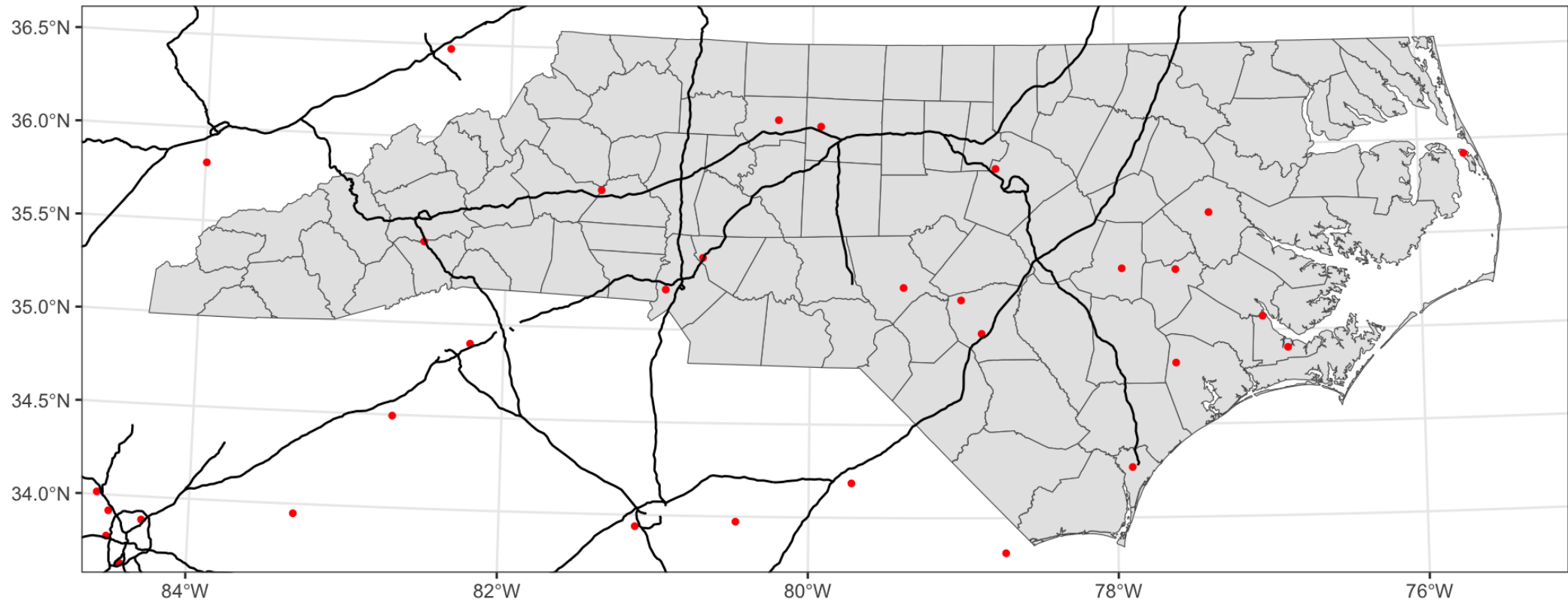
```
logi [1:100, 1:940] FALSE FALSE FALSE FALSE FALSE FALSE ...
```

Examples

- Which counties have an airport?
- Which counties are adjacent to Durham County?
- Which counties have more than 4 neighbors?

```
1 ncc = read_sf("data/gis/nc_counties/", quiet=TRUE) |> st_transform(3631)
2 air = read_sf("data/gis/airports/", quiet=TRUE) |> st_transform(3631)
3 hwy = read_sf("data/gis/us_interstates/", quiet=TRUE) |> st_transform(3631)
```

Data



Which counties have an airport?

```
1 ncc |>
2   select(COUNTY, geometry) |>
3   mutate(
4     airports = st_intersects(ncc, air) |> unclass(),
5     n = purrr::map_int(airports, length),
6     airport_names = purrr::map_chr(
7       airports,
8       ~ paste(air$AIRPT_NAME[.x], collapse=" ", " ") |> str_to_title()
9     )
10  ) |>
11  filter(n > 0) |>
12  arrange(desc(n))
```

Which counties have an airport?

Simple feature collection with 16 features and 4 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: 257742.1 ymin: 20311.68 xmax: 930352.8 ymax: 280007

Projected CRS: NAD83(NSRS2007) / North Carolina

A tibble: 16 × 5

COUNTY	geometry	airports	n	airport_names
<chr>	<MULTIPOLYGON [m]>	<list>	<int>	<chr>
1 Craven County	(((815892.7 133083, 815712 132990.1, 8...	<int>	2	Cherry Point...
2 Cumberland County	(((634732.8 168173.4, 634781.1 168150....	<int>	2	Pope Air For...
3 Forsyth County	(((480355.6 279558.3, 480622.3 279554....	<int>	1	Smith Reynol...
4 Guilford County	(((516951.1 278659.3, 517346.4 278644....	<int>	1	Piedmont Tri...
5 Dare County	(((925331.7 195868.4, 925150.9 195670....	<int>	1	Dare County ...
6 Wake County	(((635486.1 258098.2, 635729.3 258098....	<int>	1	Raleigh-Durh...
7 Pitt County	(((756611.7 231604, 757952.2 231061.2,...	<int>	1	Pitt-Greenvi...
8 Catawba County	(((416107.9 232317.8, 416052.5 231678....	<int>	1	Hickory Regi...
9 Buncombe County	(((304720 234673.2, 304825.7 234591.9,...	<int>	1	Asheville Re...
10 Wayne County	(((700246.7 204130.8, 700364.9 204087....	<int>	1	Seymour John...
11 Mecklenburg County	(((446654.6 196384.3, 446836 196381, 4...	<int>	1	Charlotte/Do...
12 Moore County	(((577854 196164.2, 577890.8 195888.4,...	<int>	1	Moore County...
13 Cabarrus County	(((453375.4 196276.2, 453511.2 196262....	<int>	1	Concord Regi...
14 Transylvania County	(((740420 0 105012 4, 740420 0 105045 ...	<int>	1	Winston-Salem

Which counties neighbor Durham County?

```
1 ncc |>
2   select(COUNTY, geometry) |>
3   mutate(
4     touch_durham = st_touches(ncc, ncc |> filter(COUNTY == "Durham County")) |> unclass(),
5     n_touches = map_int(touch_durham, length)
6   ) |>
7   filter(n_touches > 0)
```

Simple feature collection with 5 features and 3 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: 559195.8 ymin: 195938.7 xmax: 676918.6 ymax: 309925.7

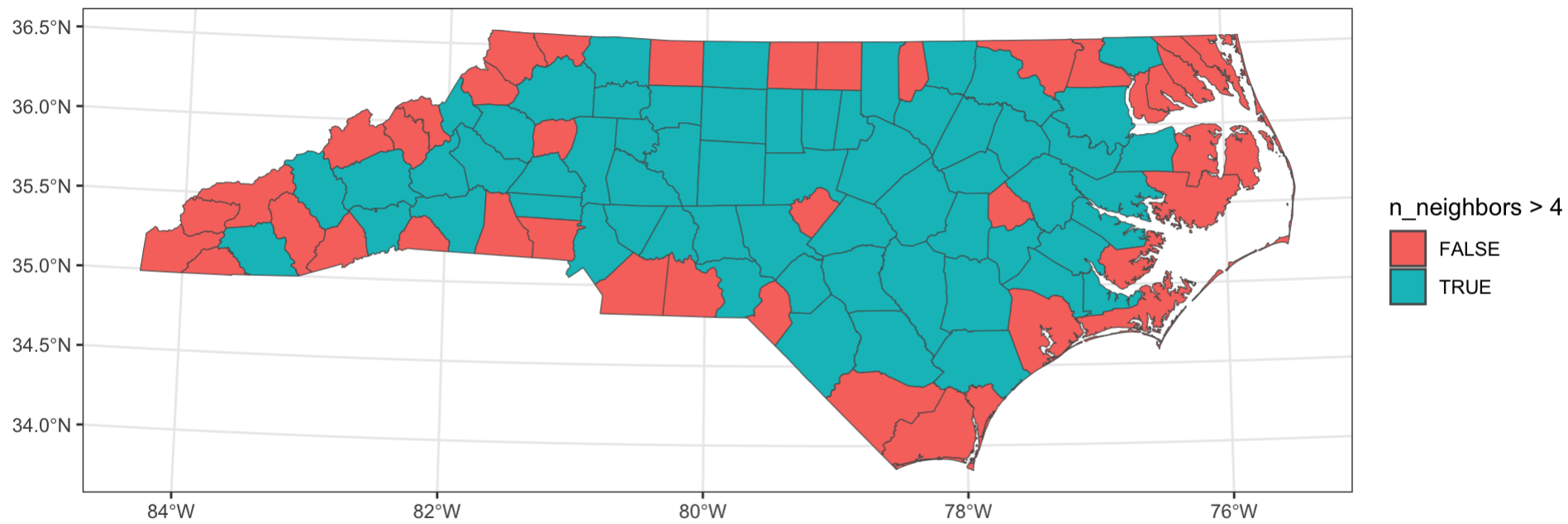
Projected CRS: NAD83(NSRS2007) / North Carolina

A tibble: 5 × 4

COUNTY	geometry	touch_durham	n_touches
* <chr>	<MULTIPOLYGON [m]>	<list>	<int>
1 Person County	(((611470.1 309761.9, 611935.8 309762, 612123.9...	<int [1]>	1
2 Granville County	(((658298.4 309773.1, 658351.6 309762.4, 658405...	<int [1]>	1
3 Orange County	(((586623.3 276687.6, 587090.7 276675.3, 587378...	<int [1]>	1
4 Wake County	(((635486.1 258098.2, 635729.3 258098.9, 635815...	<int [1]>	1
5 Chatham County	(((589371.3 235671.1, 589560.8 235648.5, 589606...	<int [1]>	1

Which counties have more than 4 neighbors?

```
1 ncc |>
2   mutate(
3     neighbors = st_touches(ncc) |> unclass(),
4     n_neighbors = map_int(neighbors, length)
5   ) |>
6   ggplot(aes(fill = n_neighbors > 4)) +
7     geom_sf()
```



Geometry Manipulation

Casting

```
1 (nc_pts = st_cast(nc, "MULTIPOINT"))
```

Simple feature collection with 100 features and 7 fields

Geometry type: MULTIPOINT

Dimension: XY

Bounding box: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965

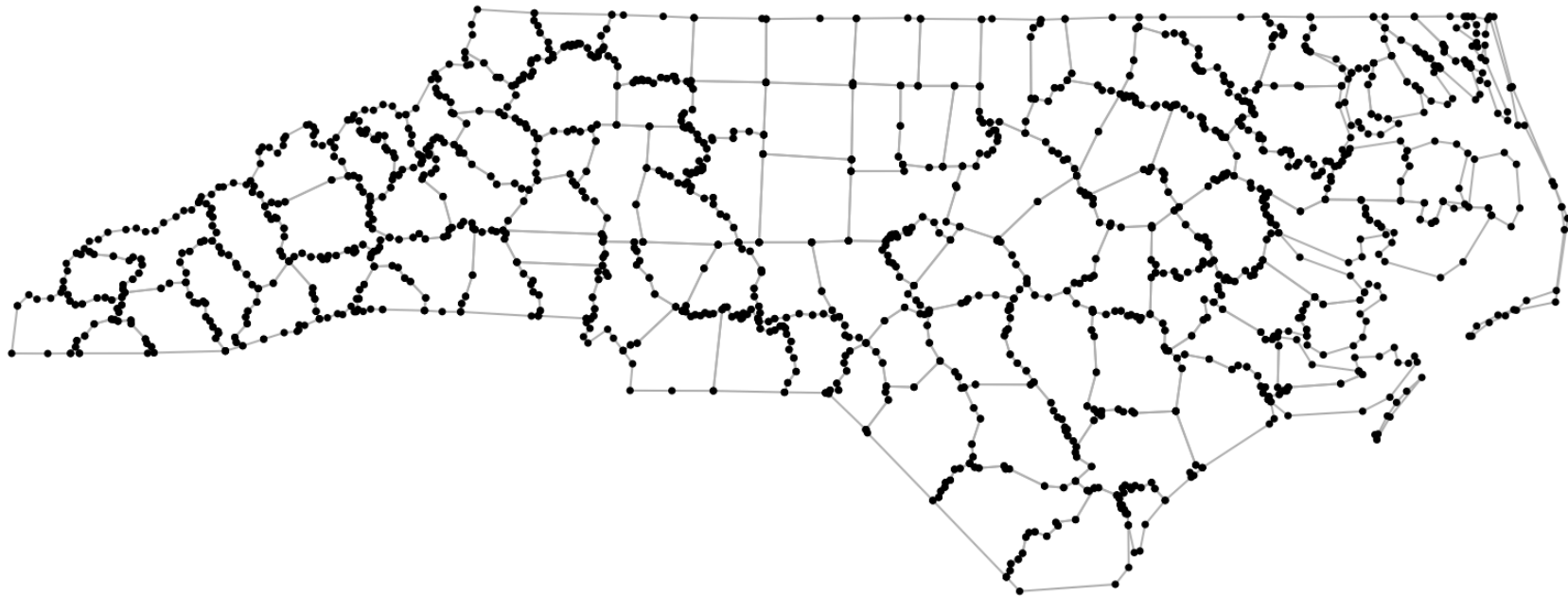
Geodetic CRS: NAD27

A tibble: 100 × 8

	NAME	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79	geometry
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<MULTIPOINT [°]>
1	Ashe	1091	1	10	1364	0	19	((-81.47276 36.23436), (-81.54084 ...
2	Alleghany	487	0	10	542	3	12	((-81.23989 36.36536), (-81.24069 ...
3	Surry	3188	5	208	3616	6	260	((-80.45634 36.24256), (-80.47639 ...
4	Currituck	508	1	123	830	2	145	((-76.00897 36.3196), (-76.01735 3...
5	Northampton	1421	9	1066	1606	3	1197	((-77.21767 36.24098), (-77.23461 ...
6	Hertford	1452	7	954	1838	5	1237	((-76.74506 36.23392), (-76.98069 ...
7	Camden	286	0	115	350	2	139	((-76.00897 36.3196), (-75.95718 3...
8	Gates	420	0	254	594	2	371	((-76.56251 36.34057), (-76.60424 ...
9	Warren	968	4	748	1190	2	844	((-78.30876 36.26004), (-78.28293 ...
10	Stokes	1612	1	160	2038	5	176	((-80.02567 36.25023), (-80.45301 ...

i 90 more rows

```
1 plot(st_geometry(nc), border='grey')  
2 plot(st_geometry(nc_pts), pch=16, cex=0.5, add=TRUE)
```



Casting - POINT

```
1 st_cast(nc, "POINT")
```

Simple feature collection with 2529 features and 7 fields

Geometry type: POINT

Dimension: XY

Bounding box: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965

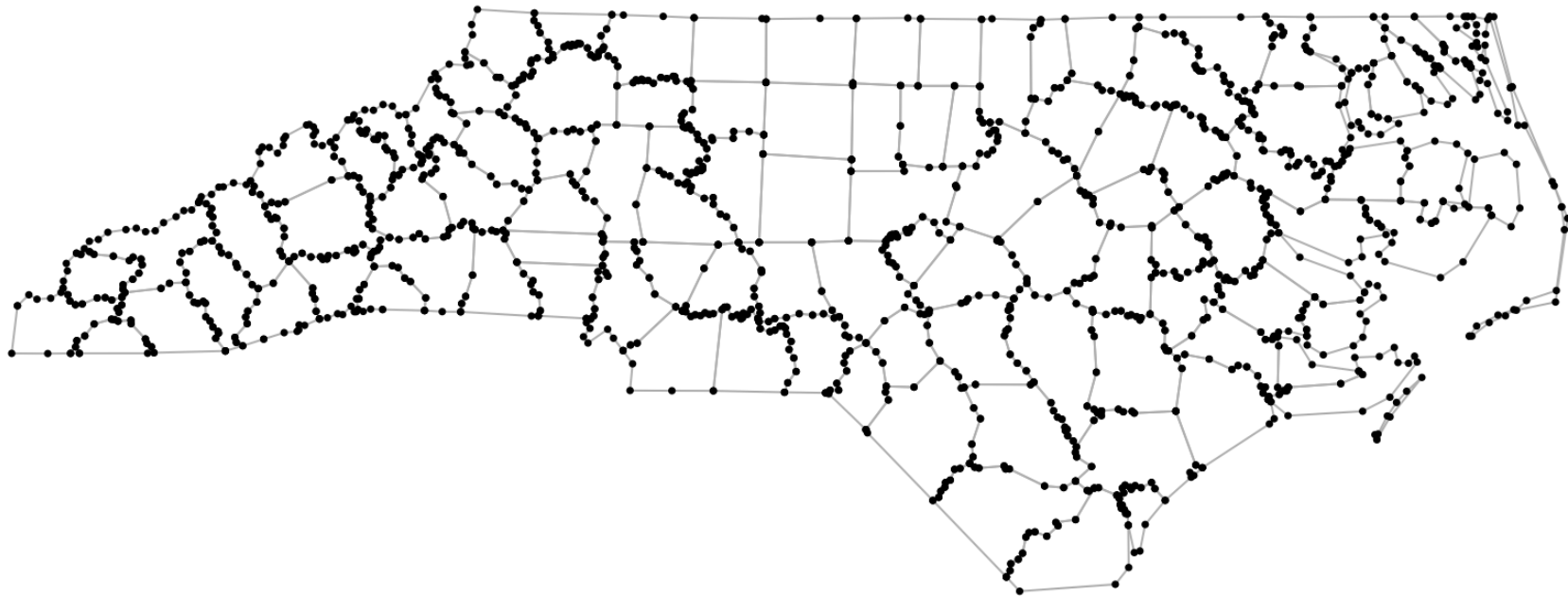
Geodetic CRS: NAD27

A tibble: 2,529 × 8

	NAME	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79	geometry
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<POINT [°]>
1	Ashe	1091	1	10	1364	0	19	(-81.47276 36.23436)
2	Ashe	1091	1	10	1364	0	19	(-81.54084 36.27251)
3	Ashe	1091	1	10	1364	0	19	(-81.56198 36.27359)
4	Ashe	1091	1	10	1364	0	19	(-81.63306 36.34069)
5	Ashe	1091	1	10	1364	0	19	(-81.74107 36.39178)
6	Ashe	1091	1	10	1364	0	19	(-81.69828 36.47178)
7	Ashe	1091	1	10	1364	0	19	(-81.7028 36.51934)
8	Ashe	1091	1	10	1364	0	19	(-81.67 36.58965)
9	Ashe	1091	1	10	1364	0	19	(-81.3453 36.57286)
10	Ashe	1091	1	10	1364	0	19	(-81.34754 36.53791)

i 2,519 more rows

```
1 plot(st_geometry(nc), border='grey')  
2 plot(st_geometry(st_cast(nc, "POINT")), pch=16, cex=0.5, add=TRUE)
```



Casting - LINESTRING

```
1 st_cast(nc, "MULTILINESTRING")
```

Simple feature collection with 100 features and 7 fields

Geometry type: MULTILINESTRING

Dimension: XY

Bounding box: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965

Geodetic CRS: NAD27

A tibble: 100 × 8

NAME	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79	geometry
<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<MULTILINESTRING [°]>
1 Ashe	1091	1	10	1364	0	19	((-81.47276 36.23436, -81.54084 36...
2 Alleghany	487	0	10	542	3	12	((-81.23989 36.36536, -81.24069 36...
3 Surry	3188	5	208	3616	6	260	((-80.45634 36.24256, -80.47639 36...
4 Currituck	508	1	123	830	2	145	((-76.00897 36.3196, -76.01735 36...
5 Northampton	1421	9	1066	1606	3	1197	((-77.21767 36.24098, -77.23461 36...
6 Hertford	1452	7	954	1838	5	1237	((-76.74506 36.23392, -76.98069 36...
7 Camden	286	0	115	350	2	139	((-76.00897 36.3196, -75.95718 36...
8 Gates	420	0	254	594	2	371	((-76.56251 36.34057, -76.60424 36...
9 Warren	968	4	748	1190	2	844	((-78.30876 36.26004, -78.28293 36...
10 Stokes	1612	1	160	2038	5	176	((-80.02567 36.25023, -80.45301 36...

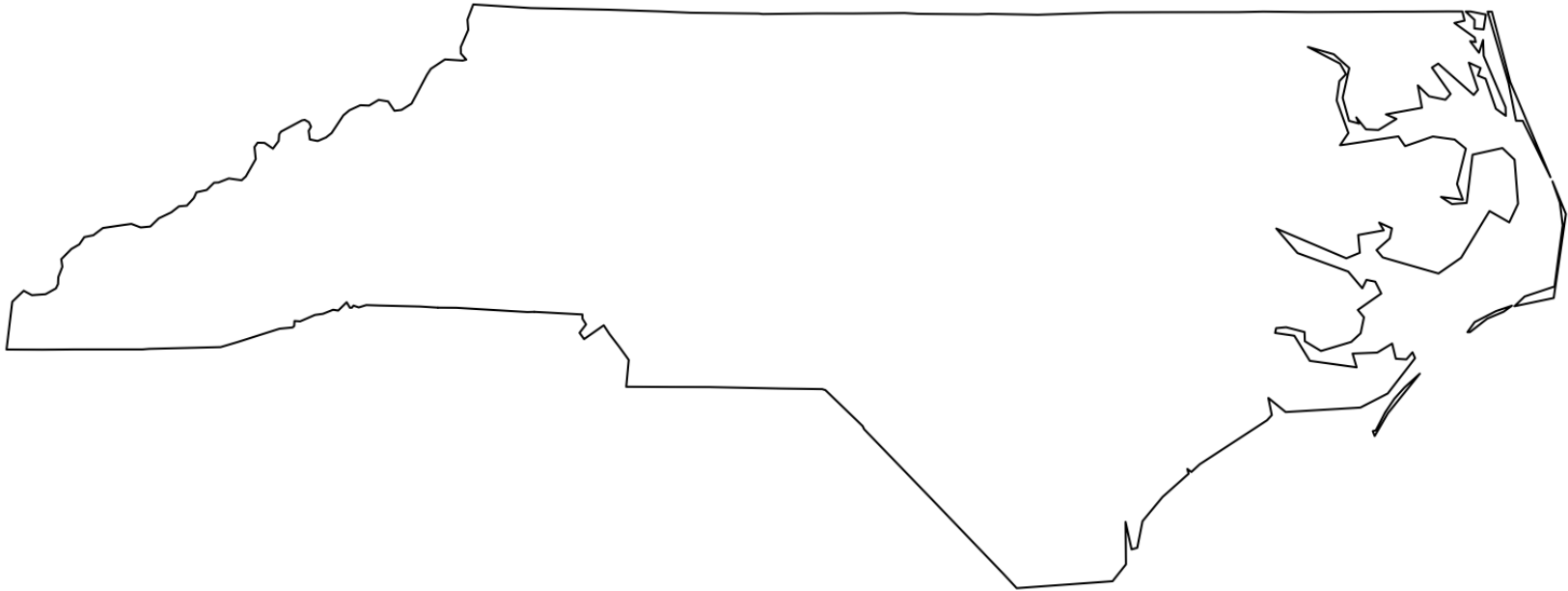
i 90 more rows

```
1 st_cast(nc, "MULTILINESTRING") |> st_geometry() |> plot()
```



Grouping Features

```
1 nc_state = st_union(nc)
2 plot(nc_state)
```



More Grouping

```
1 ( nc_cut = nc |>
2   mutate(X = st_centroid(nc) |> st_coordinates() |> (\(x) x[,1]))() |>
3   mutate(region = cut(X, breaks = 5)) )
```

Simple feature collection with 100 features and 9 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: -84.32385 ymin: 33.88199 xmax: -75.45698 ymax: 36.58965

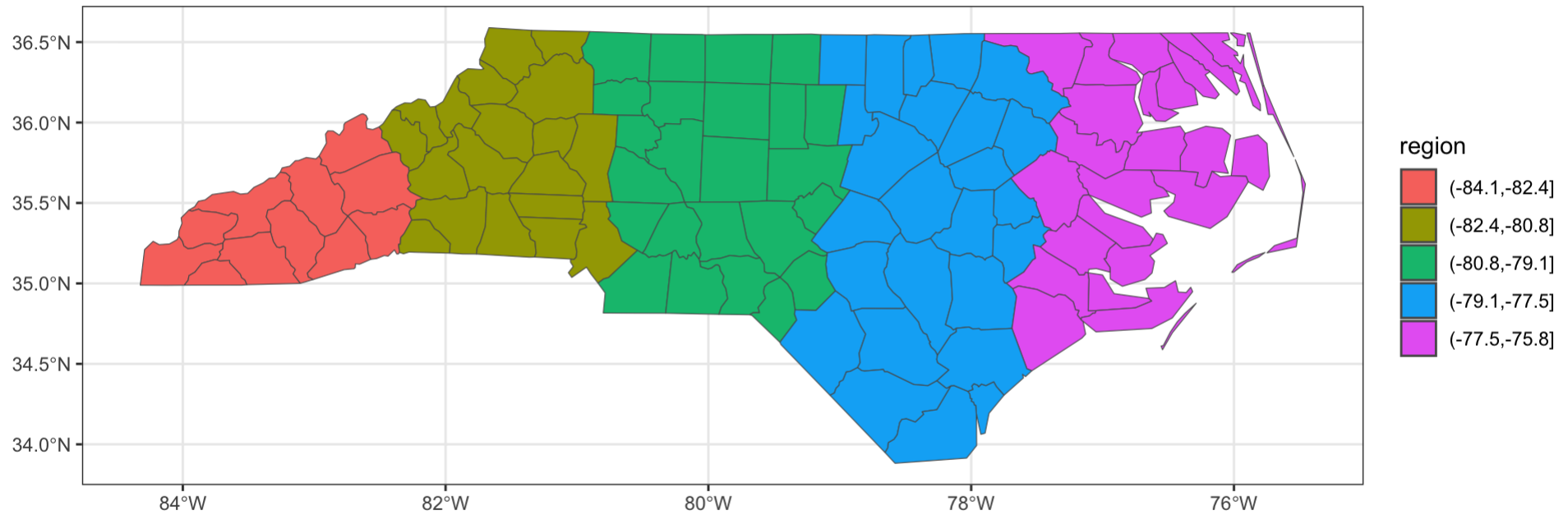
Geodetic CRS: NAD27

A tibble: 100 × 10

	NAME	BIR74	SID74	NWBIR74	BIR79	SID79	NWBIR79	geometry	X region
*	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<MULTIPOLYGON [°]>	<dbl> <fct>
1	Ashe	1091	1	10	1364	0	19	(((-81.47276 36.23436, -... -81.5 (-82....	
2	Allegha...	487	0	10	542	3	12	(((-81.23989 36.36536, -... -81.1 (-82....	
3	Surry	3188	5	208	3616	6	260	(((-80.45634 36.24256, -... -80.7 (-80....	
4	Curritu...	508	1	123	830	2	145	(((-76.00897 36.3196, -7... -76.0 (-77....	
5	Northam...	1421	9	1066	1606	3	1197	(((-77.21767 36.24098, -... -77.4 (-77....	
6	Hertford	1452	7	954	1838	5	1237	(((-76.74506 36.23392, -... -77.0 (-77....	
7	Camden	286	0	115	350	2	139	(((-76.00897 36.3196, -7... -76.2 (-77....	
8	Gates	420	0	254	594	2	371	(((-76.56251 36.34057, -... -76.7 (-77....	
9	Warren	968	4	748	1190	2	844	(((-78.30876 36.26004, -... -78.1 (-79....	
10	Stokes	1612	1	160	2038	5	176	(((-80.02567 36.25023, -... -80.2 (-80....	

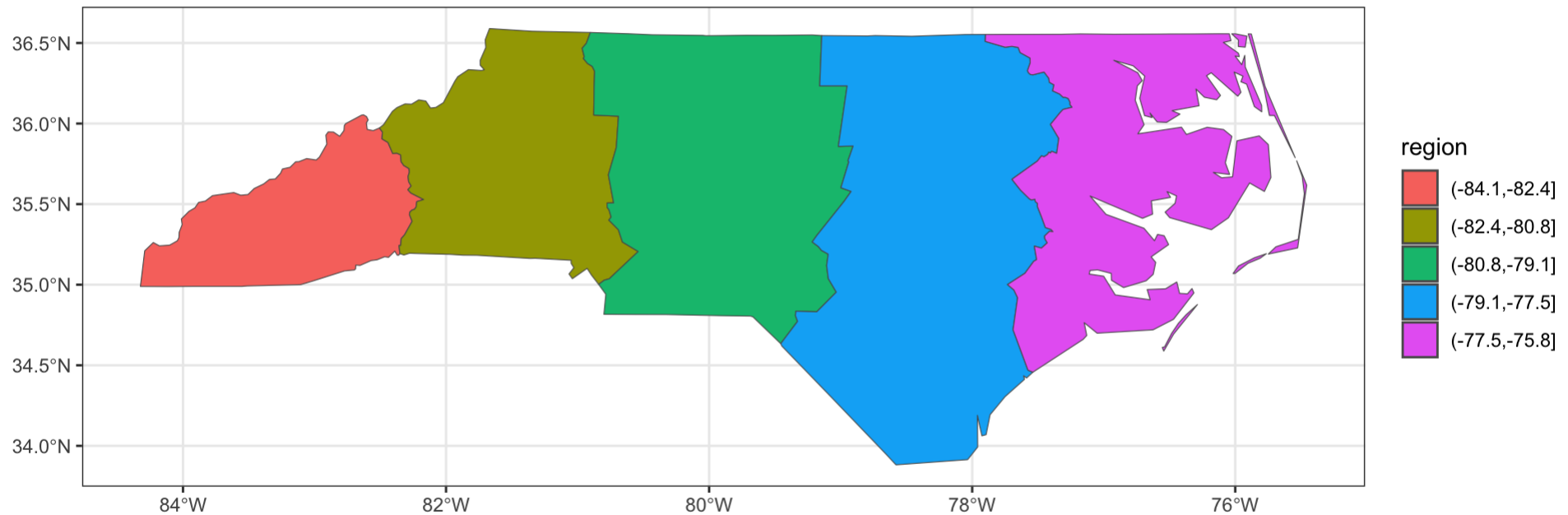
i 90 more rows

```
1 ggplot(nc_cut) +  
2   geom_sf(aes(fill=region))
```



Union via summarize

```
1 nc_cut |>
2   group_by(region) |>
3   summarize() |>
4   ggplot() +
5     geom_sf(aes(fill=region))
```



Affine Transformations

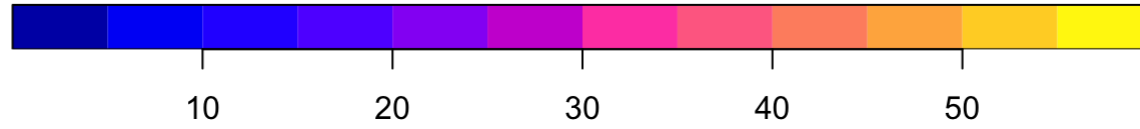
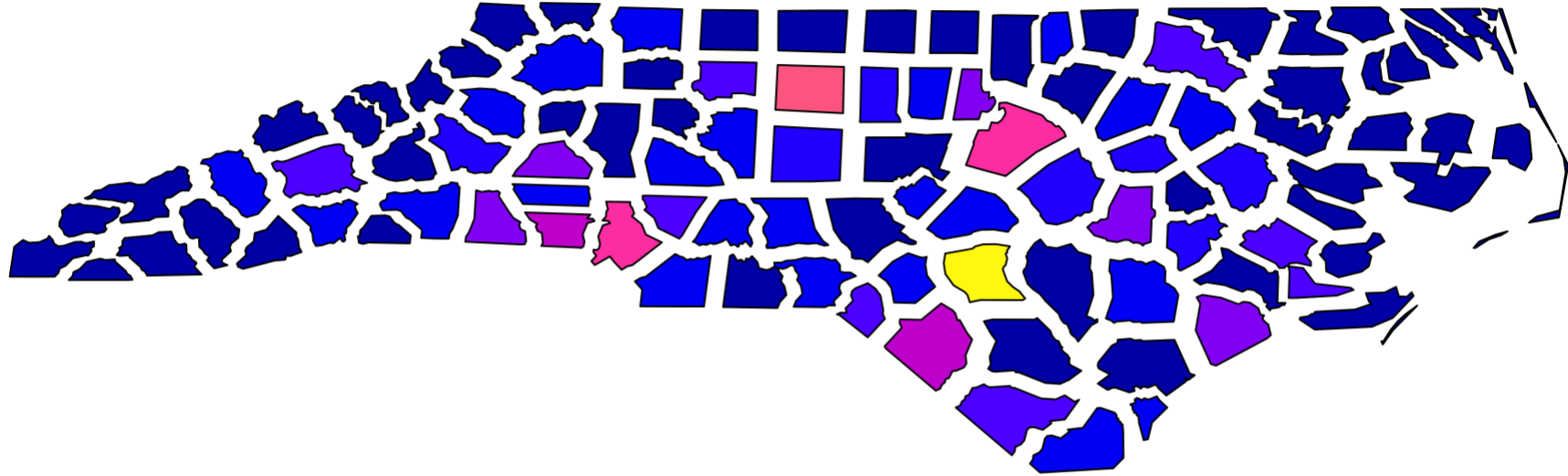
```
1 rotate = function(a) matrix(c(cos(a), sin(a), -sin(a), cos(a)), 2, 2)
2
3 ctrd = st_centroid(nc_state)
4 state_rotate = (nc_state) * rotate(-pi/4)
5 plot(state_rotate, axes=TRUE)
```



Scaling Size

```
1 ctrd = st_centroid(st_geometry(nc))
2 area = st_area(nc) |> strip_attrs()
3
4 nc_rot = nc
5 st_geometry(nc_rot) = (st_geometry(nc) - ctrd) * 0.75 + ctrd
6
7 plot(nc_rot[, "SID79"])
```

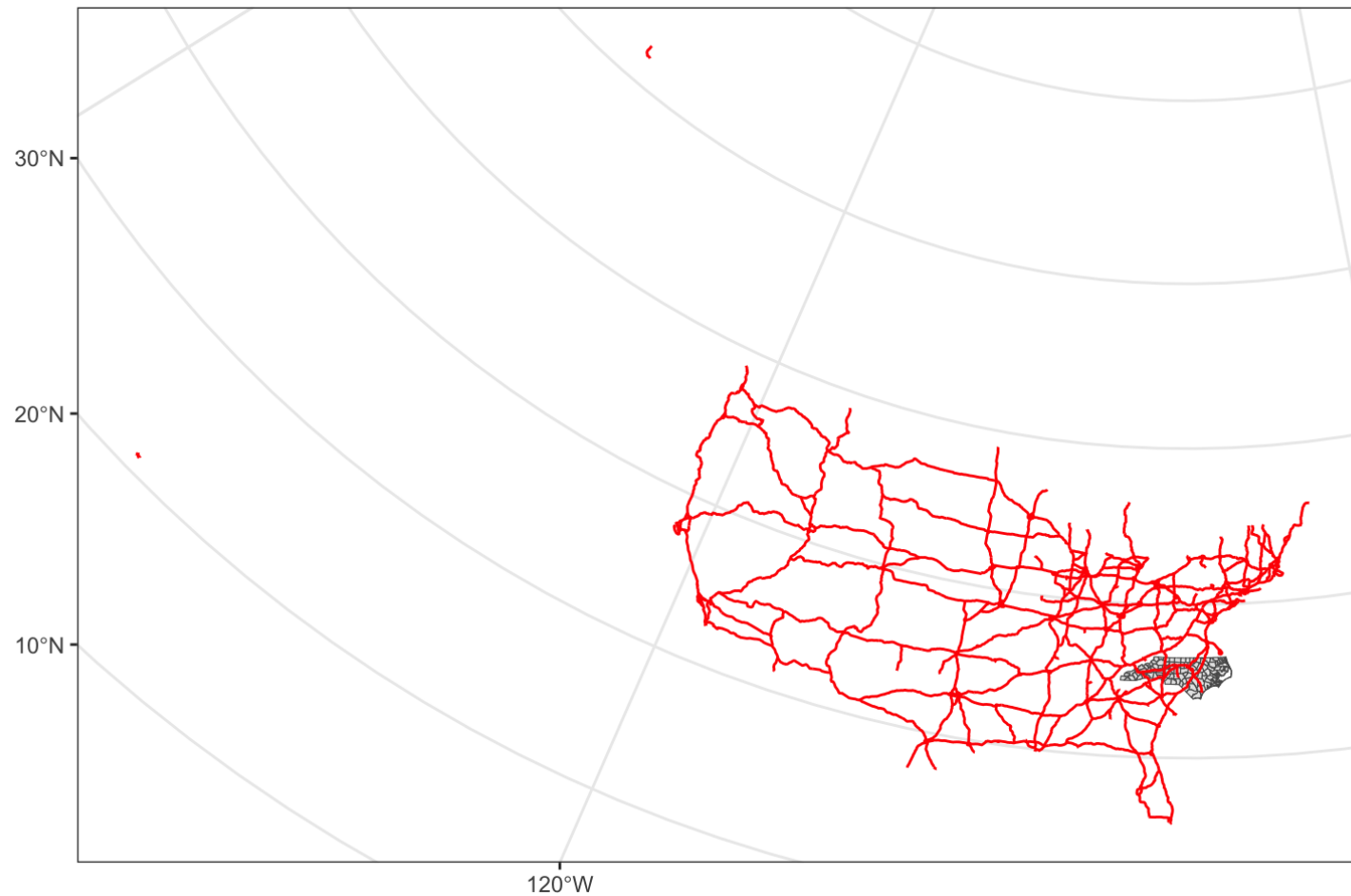
SID79



Highway Example

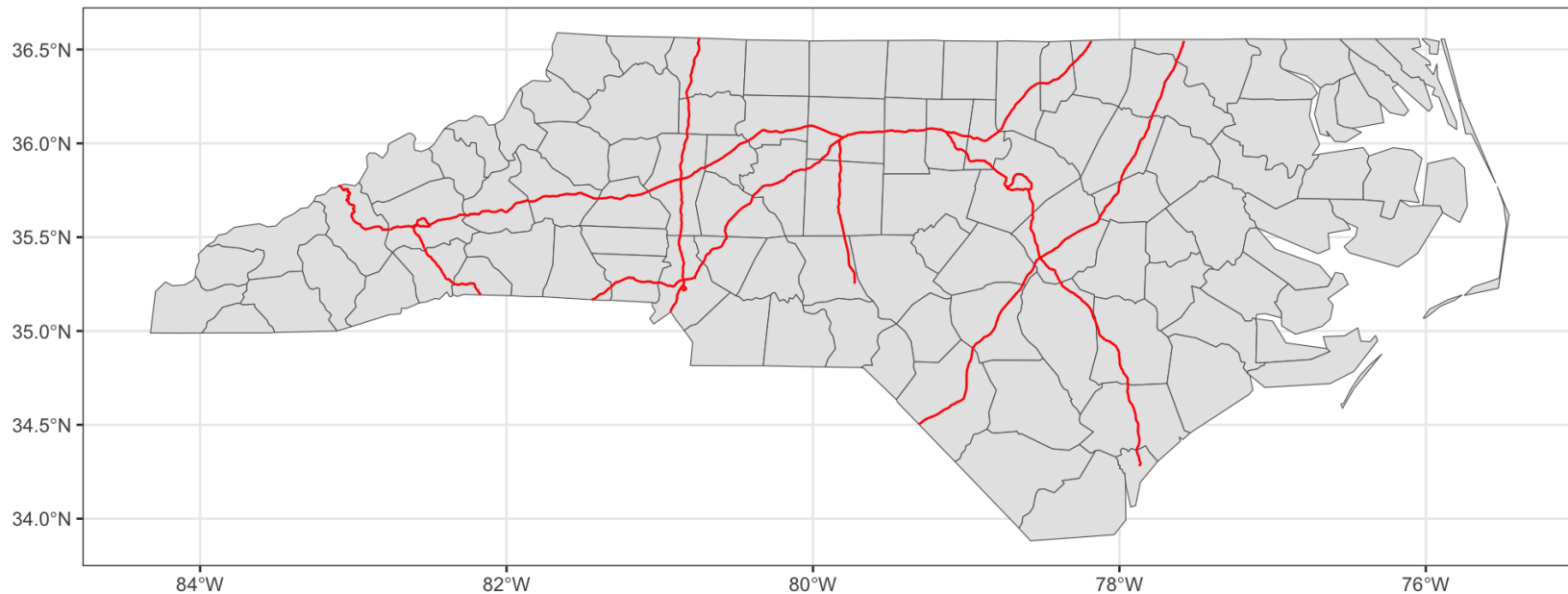
Highways

```
1 ggplot() +  
2   geom_sf(data=ncc) +  
3   geom_sf(data=hwy, col='red')
```



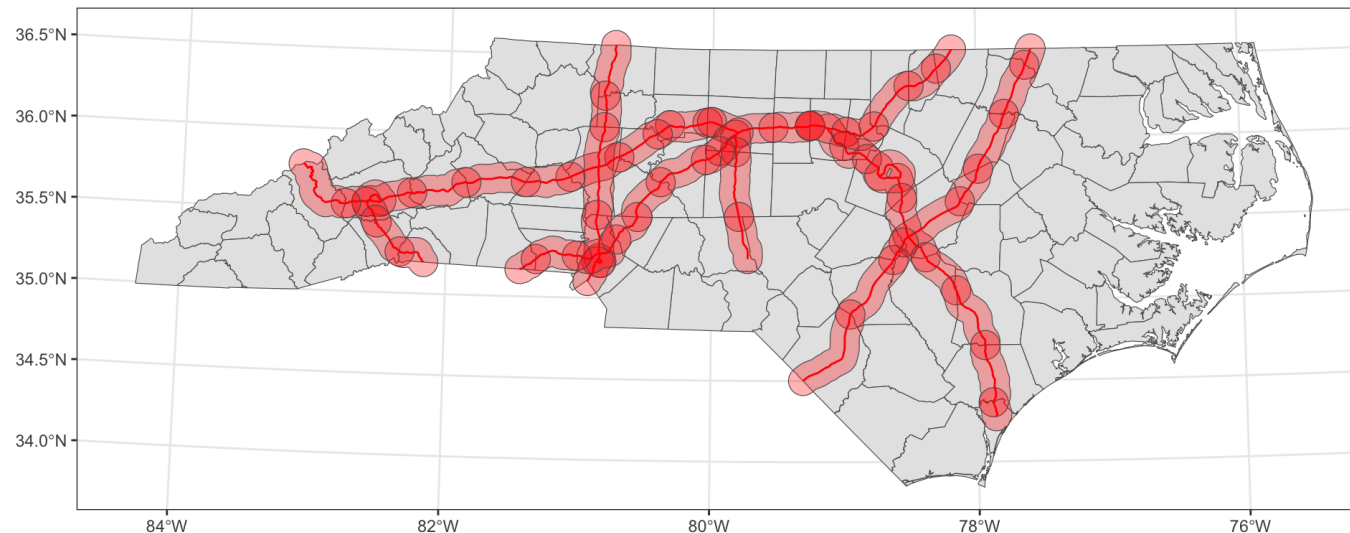
NC Interstate Highways

```
1 hwy_nc = st_intersection(hwy, ncc)
2
3 ggplot() +
4   geom_sf(data=nc) +
5   geom_sf(data=hwy_nc, col='red')
```



Counties near the interstate (Buffering)

```
1 hwy_nc_buffer = hwy_nc |>
2   st_buffer(10000)
3
4 ggplot() +
5   geom_sf(data=ncc) +
6   geom_sf(data=hwy_nc, color='red') +
7   geom_sf(data=hwy_nc_buffer, fill='red', alpha=0.3)
```



Counties near the interstate (Buffering + Union)

```
1 hwy_nc_buffer = hwy_nc |>  
2   st_buffer(10000) |>  
3   st_union() |>  
4   st_sf()
```

```
1 ggplot() +  
2   geom_sf(data=ncc) +  
3   geom_sf(data=hwy_nc, color='red') +  
4   geom_sf(data=hwy_nc_buffer, fill='red', alp
```

Example

How many counties in North Carolina are within 5, 10, 20, or 50 km of an interstate highway?

```
1 hwy_nc |>
2   st_buffer(10000) |>
3   st_union() |>
4   st_intersects(ncc, y = _) |>
5   map_lgl(~ length(.x) >= 1) |>
6   sum()
```

```
[1] 55
```

Gerrymandering Example

NC House Districts - 112th Congress

```
1 ( nc_house = read_sf("data/nc_districts112.gpkg", quiet = TRUE) |>
2   select(ID, DISTRICT) |>
3   mutate(DISTRICT = as_factor(DISTRICT))
4 )
```

Simple feature collection with 13 features and 2 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: -84.32187 ymin: 33.84452 xmax: -75.45998 ymax: 36.58812

Geodetic CRS: WGS 84

A tibble: 13 × 3

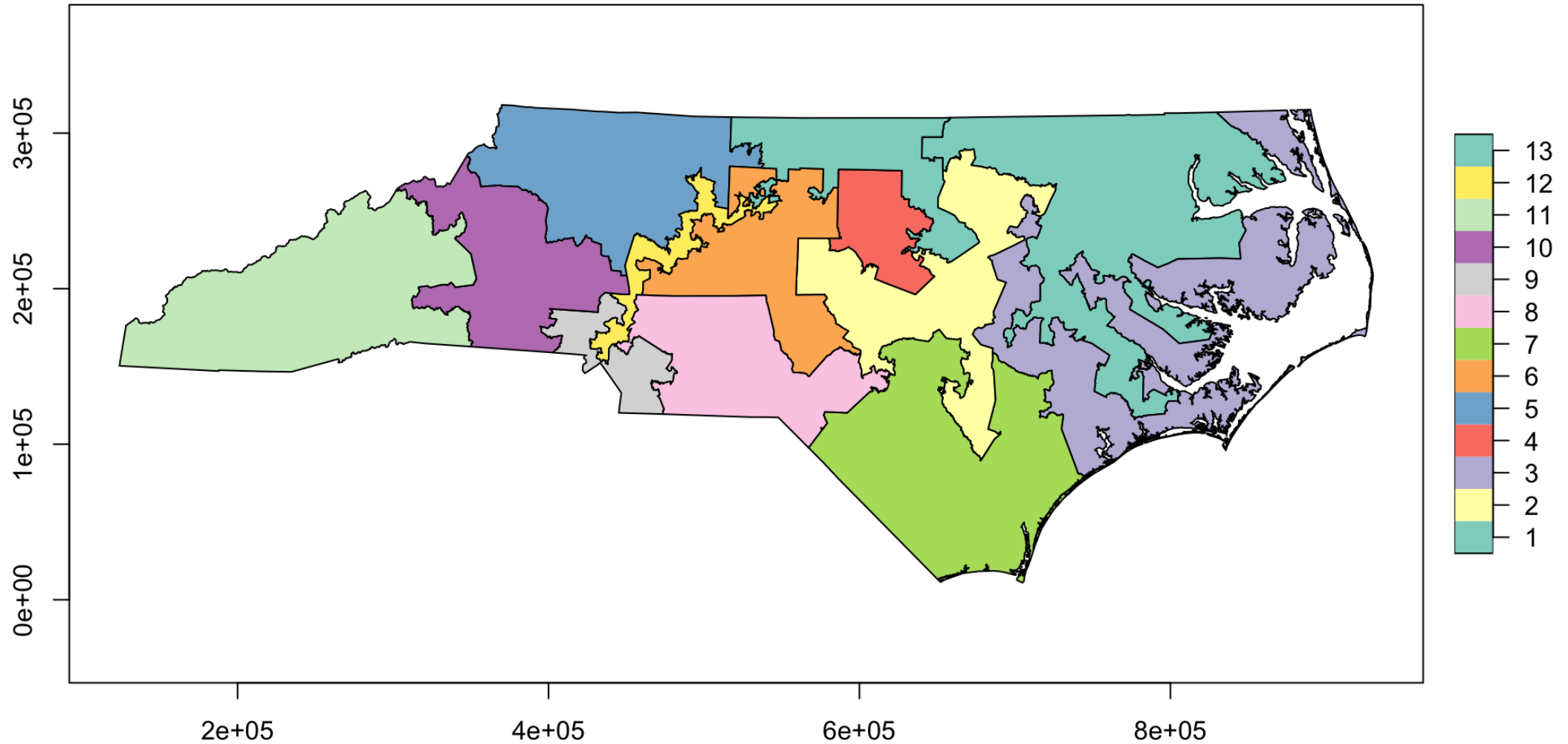
ID	DISTRICT	geom
* <chr>	<fct>	<MULTIPOLYGON [°]>
1 037108112001	1	(((-77.32845 35.35031, -77.35398 35.32799, -77.33...
2 037108112002	2	(((-78.89928 35.12619, -78.89763 35.12859, -78.89...
3 037108112003	3	(((-75.68266 35.23291, -75.68113 35.23237, -75.68...
4 037108112004	4	(((-78.77926 35.78568, -78.77947 35.77568, -78.79...
5 037108112005	5	(((-79.8968 36.38075, -79.89213 36.37108, -79.892...
6 037108112006	6	(((-80.4201 35.68953, -80.41483 35.68918, -80.411...
7 037108112007	7	(((-77.59169 34.40907, -77.58699 34.40611, -77.58...
8 037108112008	8	(((-78.93373 34.95909, -78.94074 34.95789, -78.94...

9 037108112009 9

(((-80.93058 35.18181, -80.9244 35.16754, -80.921...

```
1 nc_house = st_transform(nc_house, 3631)
2 plot(nc_house[, "DISTRICT"], axes=TRUE)
```

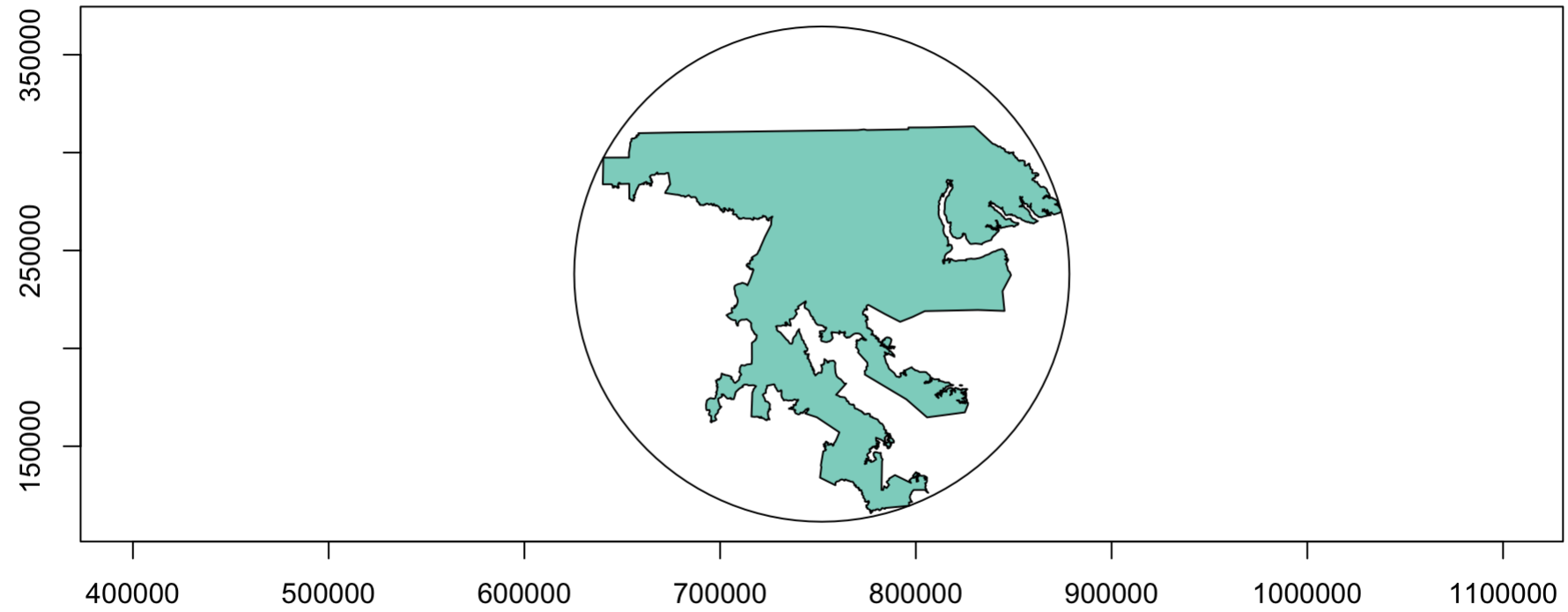
DISTRICT



Measuring Compactness - Reock Score

The Reock score is a measure of compactness that is calculated as the ratio of the area of a shape to the area of its minimum bounding circle.

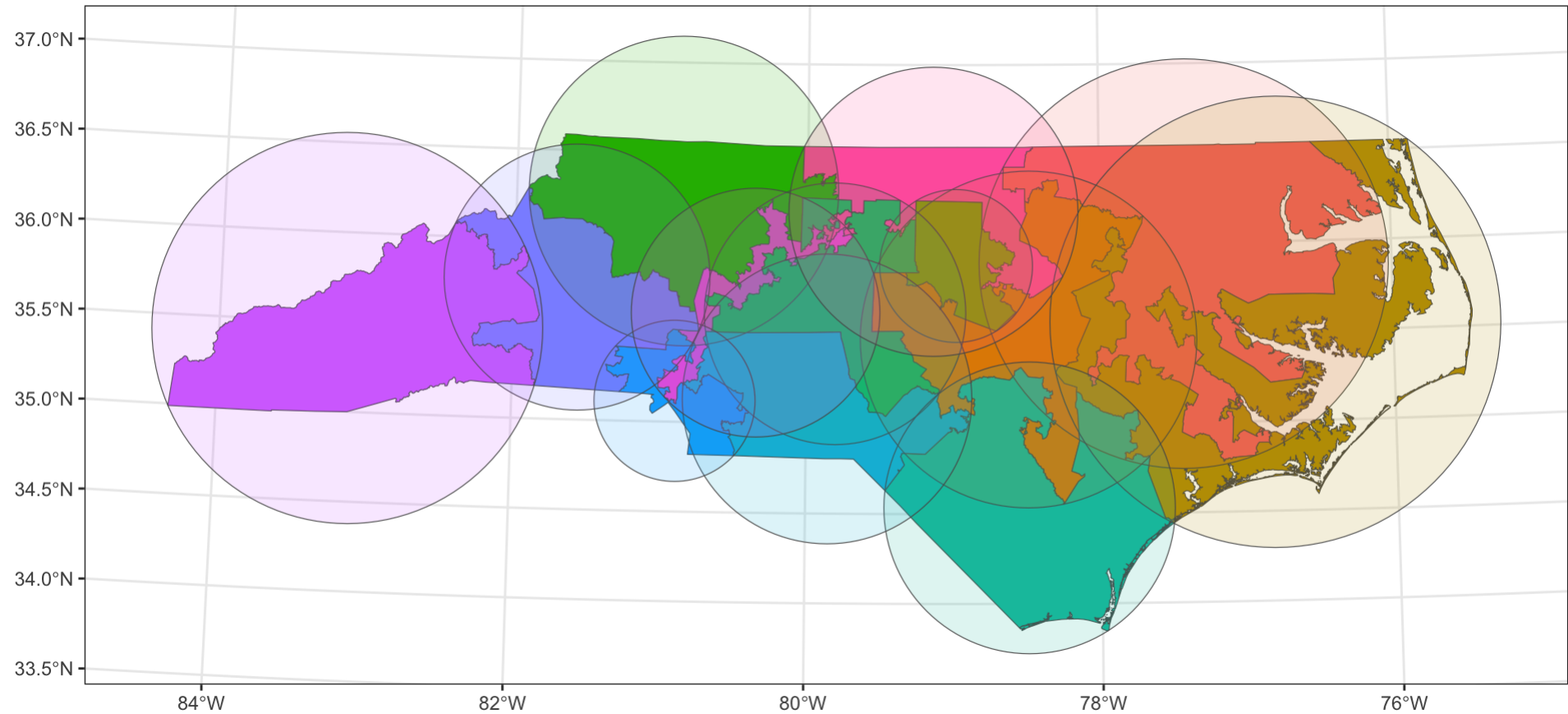
```
1  circs = nc_house |>  
2    lwgeom::st_minimum_bounding_circle()  
3  plot(circs |> filter(DISTRICT == 1) |> st_geometry(), axes=TRUE)  
4  plot(nc_house |> select(DISTRICT) |> filter(DISTRICT == 1), add=TRUE)
```



```

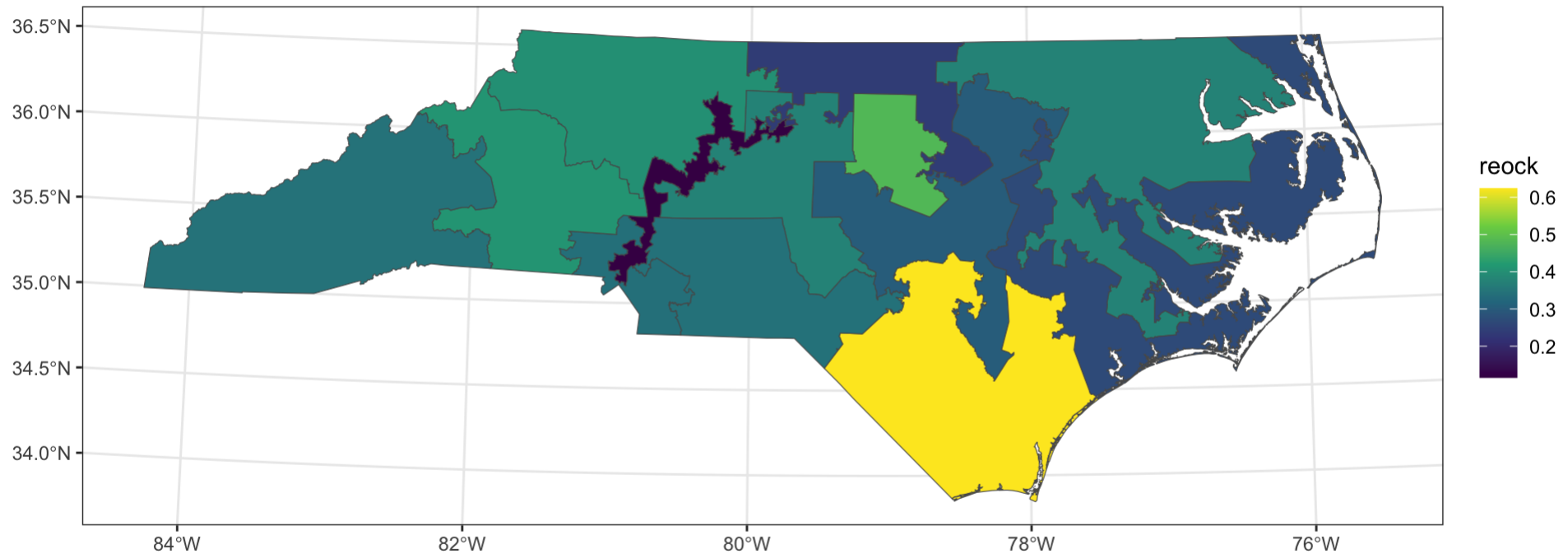
1 ggplot(mapping = aes(fill=DISTRICT)) +
2   geom_sf(data=nc_house) +
3   geom_sf(data=circls, alpha=0.15) +
4   guides(color="none", fill="none")

```



Calculating Reock

```
1 nc_house |>  
2   mutate(reock = (st_area(nc_house) / st_area(circs)) |> as.numeric()) |>  
3   ggplot(aes(fill = reock)) +  
4     geom_sf() +  
5     scale_fill_viridis_c()
```



```

1 nc_house |>
2   mutate(reock = st_area(nc_house) / st_area(circs)) |>
3   arrange(reock) |>
4   print(n=13)

```

Simple feature collection with 13 features and 3 fields

Geometry type: MULTIPOLYGON

Dimension: XY

Bounding box: xmin: 123998.5 ymin: 10979.77 xmax: 930346 ymax: 318095.3

Projected CRS: NAD83(NSRS2007) / North Carolina

A tibble: 13 × 4

ID	DISTRICT	geom	reock
<chr>	<fct>	<MULTIPOLYGON [m]>	[1]
1 037108112012	12	((473814.9 211717.3, 472007.4 209951.4, 47...	0.116
2 037108112013	13	((528146.8 292339.5, 528222.3 292562.4, 52...	0.237
3 037108112003	3	((911479.9 169543.9, 911621.3 169488.3, 91...	0.266
4 037108112002	2	((618780.6 152664.8, 618930.2 152932.2, 61...	0.303
5 037108112009	9	((433786.4 160540.2, 434318.7 158946.9, 43...	0.339
6 037108112008	8	((615653.2 134126.5, 615013 133993.3, 6147...	0.342
7 037108112011	11	((154791.1 191470.8, 154769.4 192168.1, 15...	0.344
8 037108112006	6	((481076.7 216074.5, 481553 216028, 481879...	0.378
9 037108112001	1	((761514.7 178801.2, 759235.4 176286.8, 76...	0.378
10 037108112005	5	((529128.7 292213.3, 529538 291136.4, 5294...	0.399
11 037108112010	10	((424301.6 185435.1, 400728.7 187075, 4018...	0.411
12 037108112004	4	((629556.3 225844, 629539.1 224734.4, 6281...	0.480
13 037108112007	7	((739073.9 74030.77, 739510.2 73709.48, 73...	0.624

Raster Data (stars)

Example data - Meuse

```
1 ( meuse_rast = stars::read_stars(  
2   system.file("external/test.grd", package="raster")  
3 ) |>  
4   st_transform(st_crs(meuse_riv))  
5 )
```

stars object with 2 dimensions and 1 attribute

attribute(s):

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's
test.grd	138.7071	293.9575	371.9001	425.606	501.0102	1736.058	6022

dimension(s):

	from	to	refsys	values	x/y
x	1	80	Amersfoort / RD New	[80x115] 178451,...,181611	[x]
y	1	115	Amersfoort / RD New	[80x115] 329530,...,334090	[y]

curvilinear grid

stars class

```
1 str(meuse_rast)
```

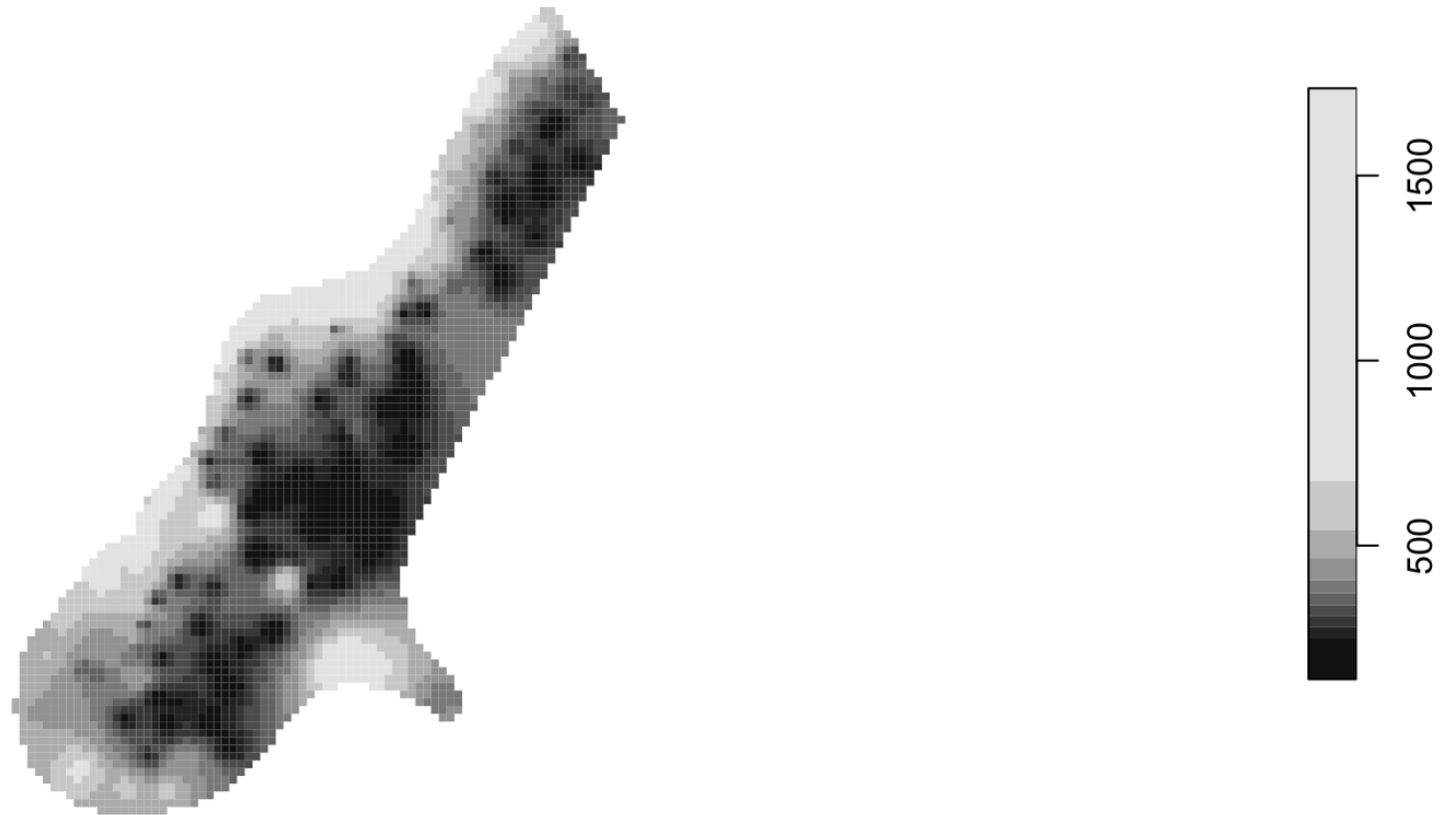
List of 1

```
$ test.grd: num [1:80, 1:115] NA NA NA NA NA NA NA NA NA NA ...  
- attr(*, "dimensions")=List of 2  
..$ x:List of 7  
.. ..$ from : num 1  
.. ..$ to   : num 80  
.. ..$ offset: num NA  
.. ..$ delta : num NA  
.. ..$ refsyz:List of 2  
.. .. ..$ input: chr "EPSG:28992"  
.. .. ..$ wkt   : chr "PROJCRS[\"Amersfoort / RD New\", \n      BASEGEOGCRS[\"Amersfoort\", \n      DATUM[\"Amersfoort\", \n      E\"| __truncated__  
.. .. ..- attr(*, \"class\")= chr \"crs\"  
.. ..$ point : logi NA  
.. ..$ values: num [1:80, 1:115] 178451 178491 178531 178571 178611 ...  
.. ..- attr(*, \"class\")= chr \"dimension\"  
..$ y:List of 7  
.. ..$ from : num 1  
.. ..$ to   : num 115  
.. ..$ offset: num NA  
.. ..$ delta : num NA  
* reference system of 2
```

Plotting

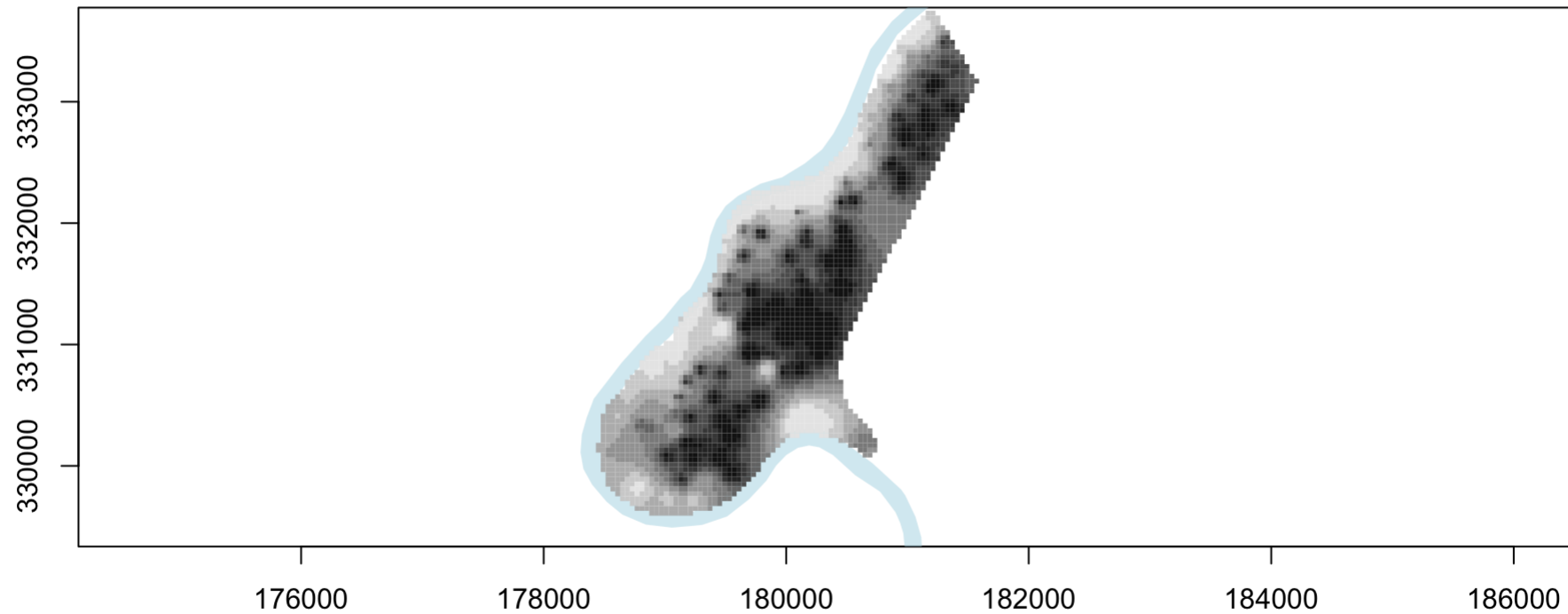
```
1 plot(meuse_rast)
```

test.grd



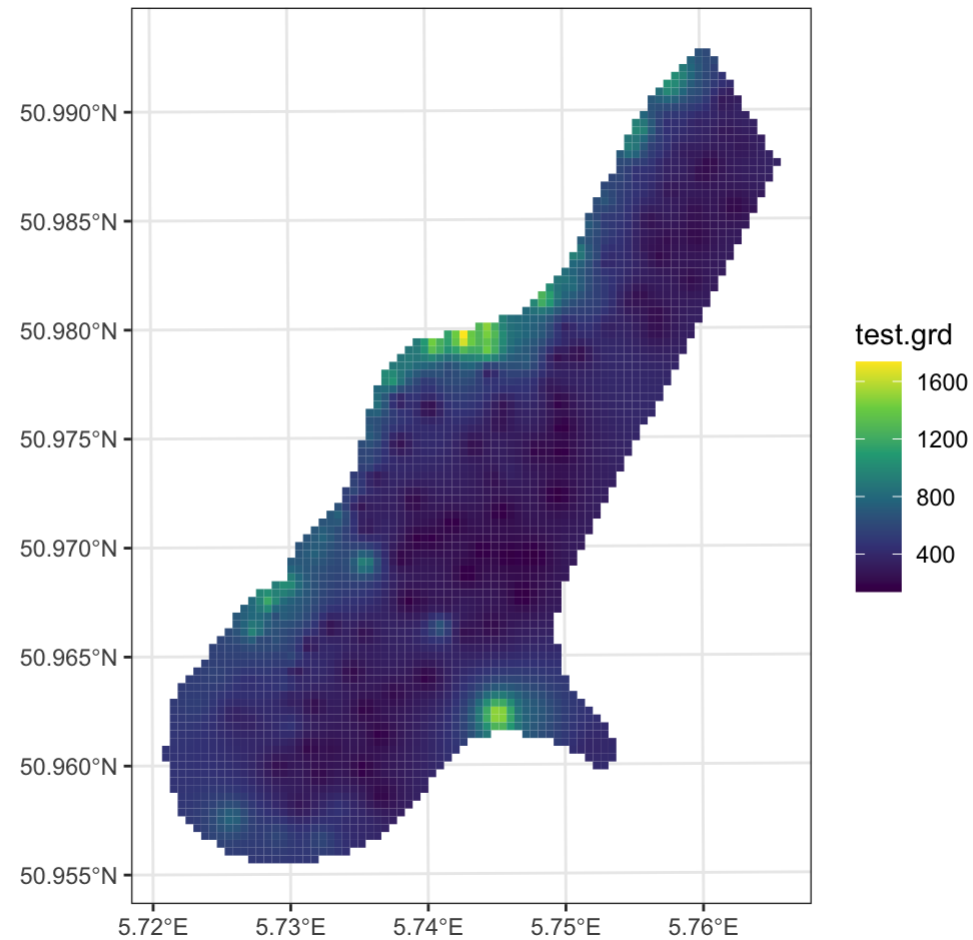
```
1 plot(  
2   meuse_riv,  
3   col=adjustcolor("lightblue",alpha.f = 0.5), border=NA,  
4   ylim = c(329500, 333611), axes=TRUE  
5 )  
6 plot(meuse_rast, add=TRUE)
```

test.grd



ggplot

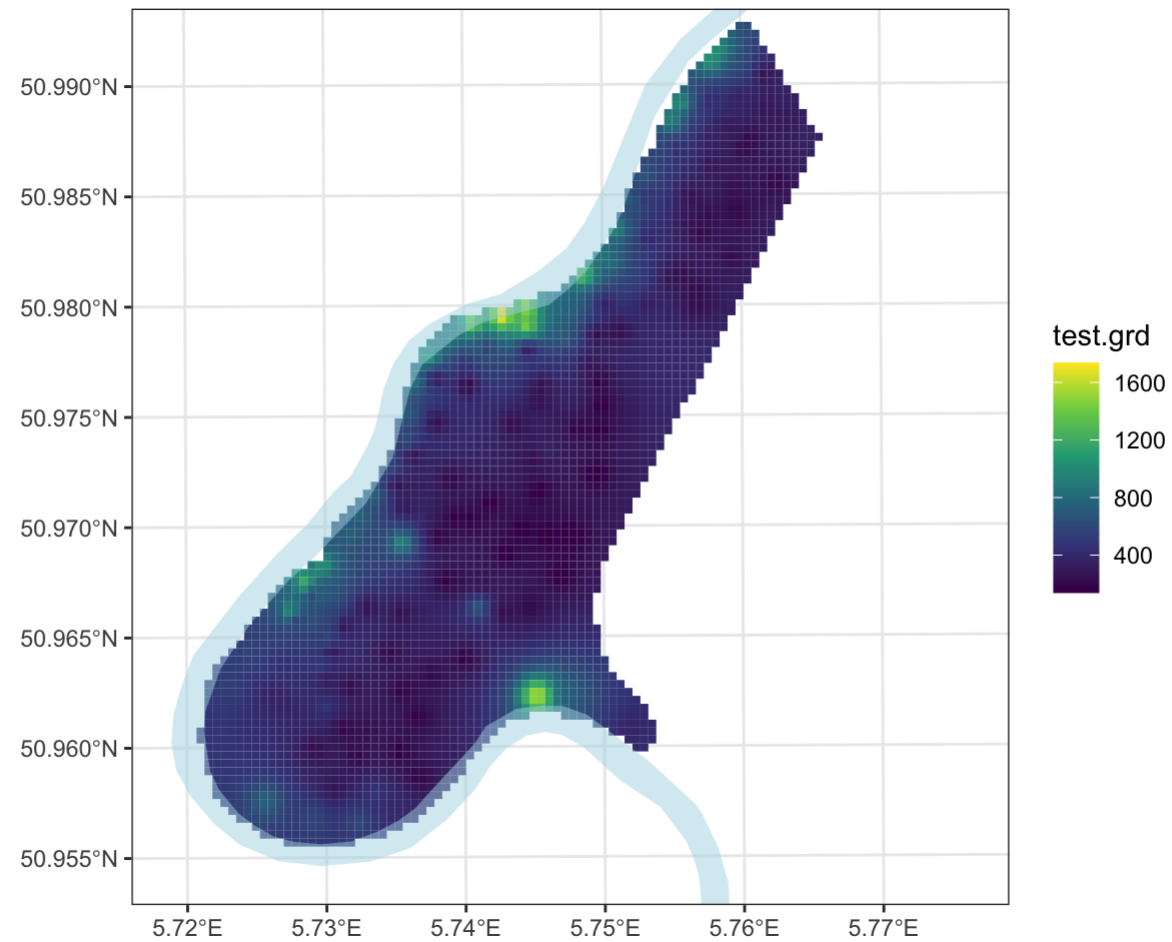
```
1 ggplot() +  
2   stars::geom_stars(data=meuse_rast) +  
3   scale_fill_viridis_c()
```



```

1 ggplot() +
2   stars::geom_stars(data=meuse_rast) +
3   geom_sf(data=meuse_riv, fill="lightblue", color=NA, alpha=0.5) +
4   scale_fill_viridis_c() +
5   ylim(329500, 333611)

```

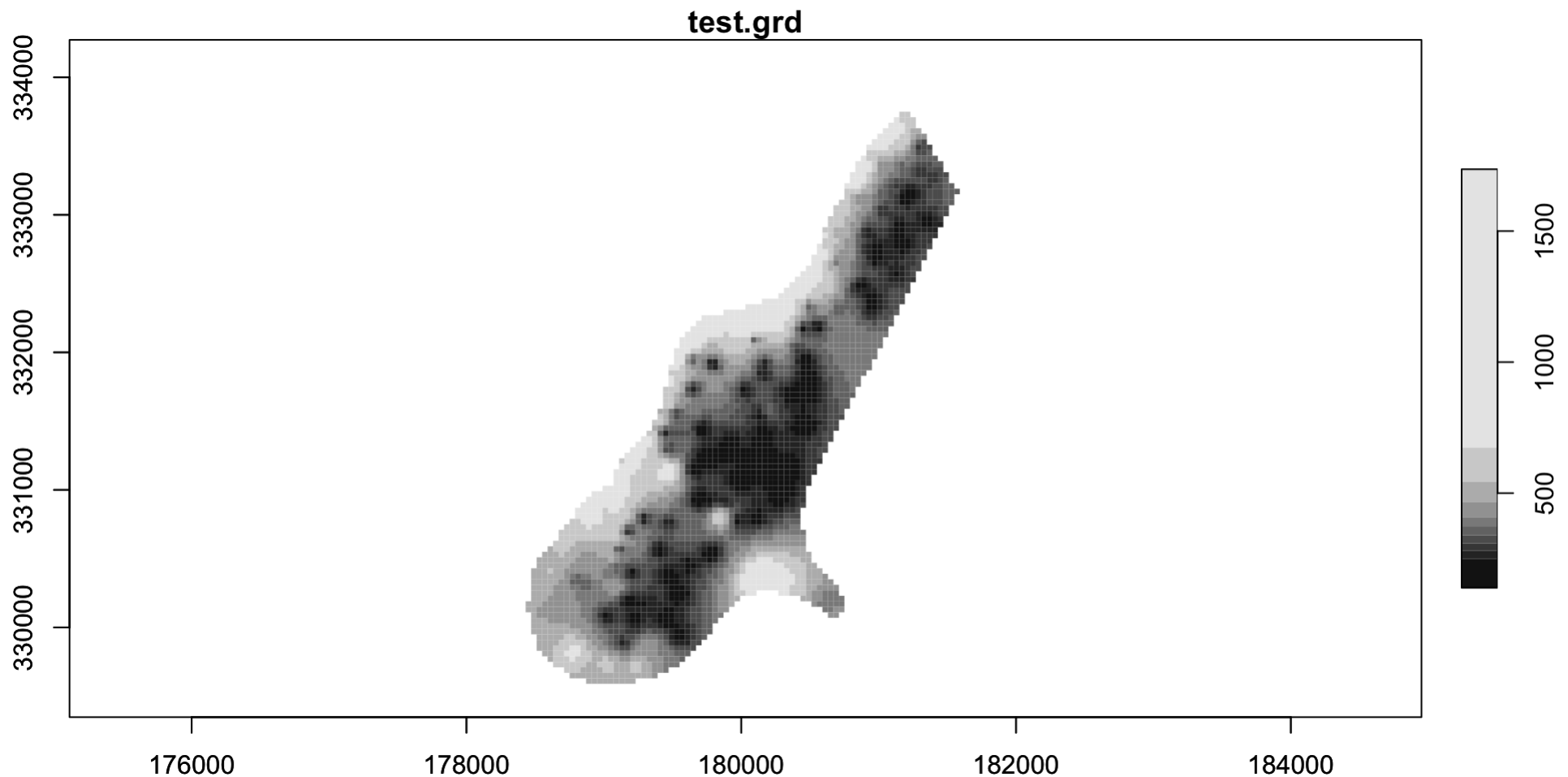


Rasters and Projections

EPSG 3631

Lat / Long

```
1 plot(meuse_rast, axes=TRUE)
```



```
1 meuse_rast
```

stars object with 2 dimensions and 1 attribute

attribute(s):

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's
test.grd	138.7071	293.9575	371.9001	425.606	501.0102	1736.058	6022

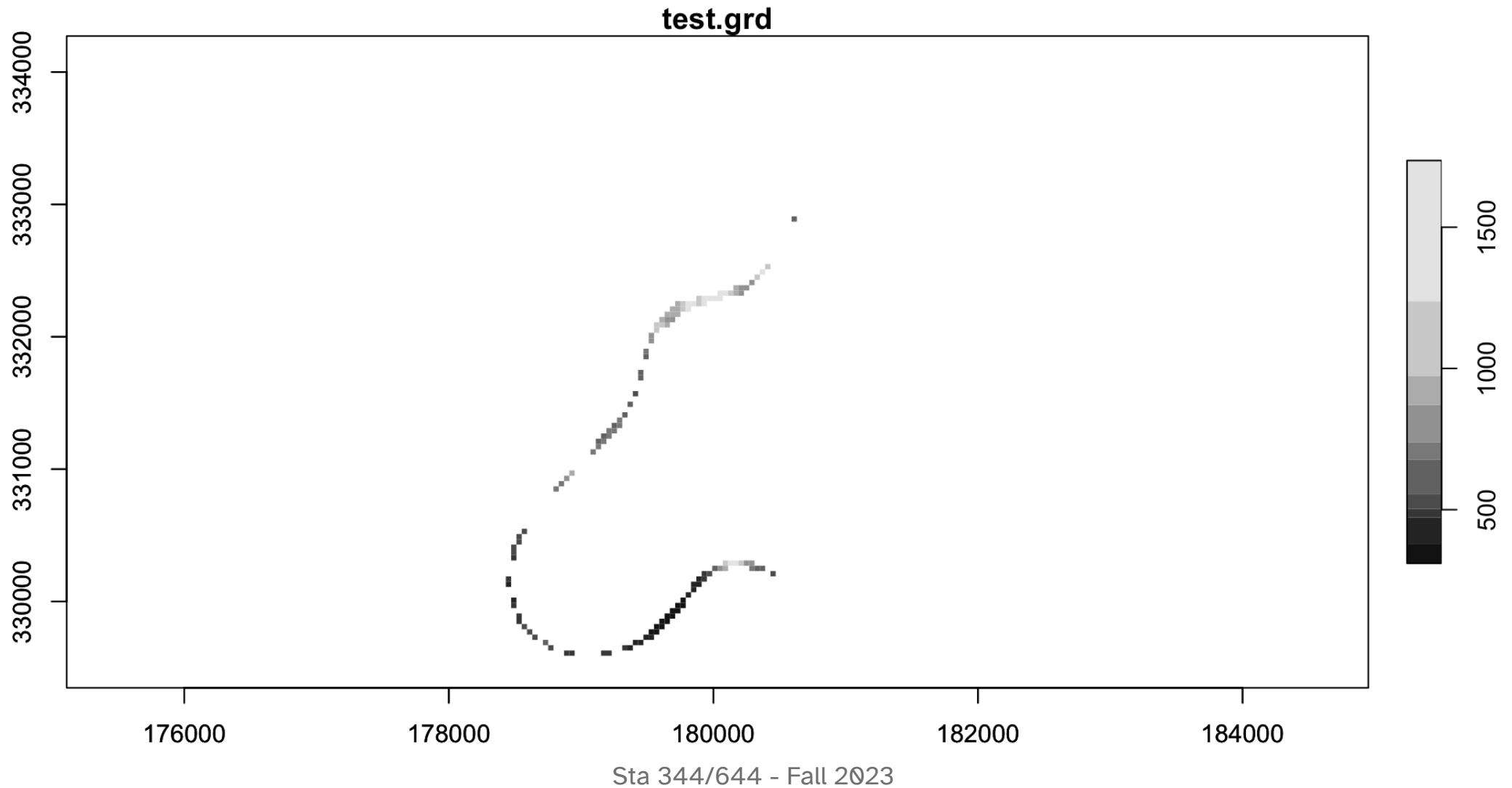
dimension(s):

	from	to	refsys	values	x/y
x	1	80	Amersfoort / RD New	[80x115] 178451,...,181611	[x]
y	1	115	Amersfoort / RD New	[80x115] 329530,...,334090	[y]

curvilinear grid

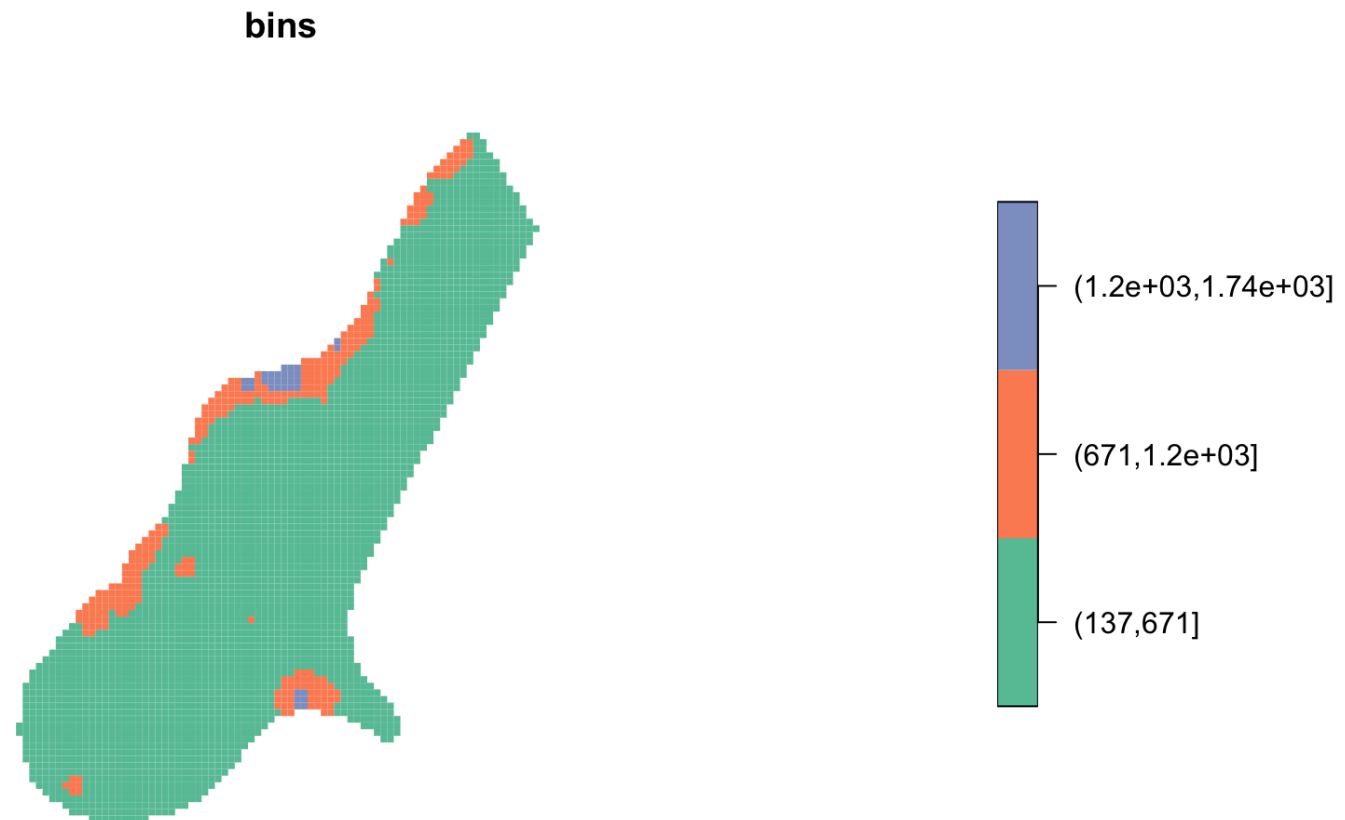
Cropping

```
1 meuse_rast_riv = meuse_rast[ meuse_riv ]  
2 plot(meuse_rast_riv, axes=TRUE)
```



Segmentation

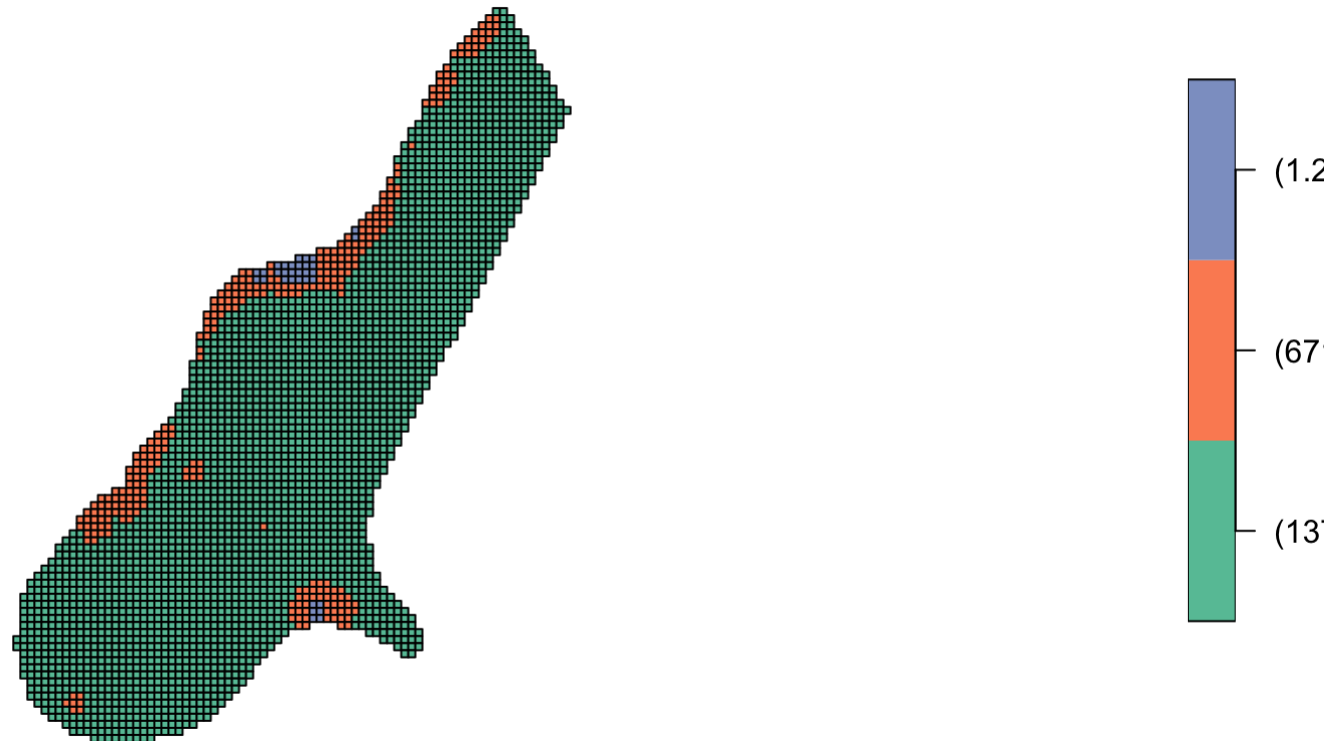
```
1 meuse_rast |>  
2   mutate(bins = cut(test.grd, 3) ) |>  
3   select(bins) |>  
4   plot()
```



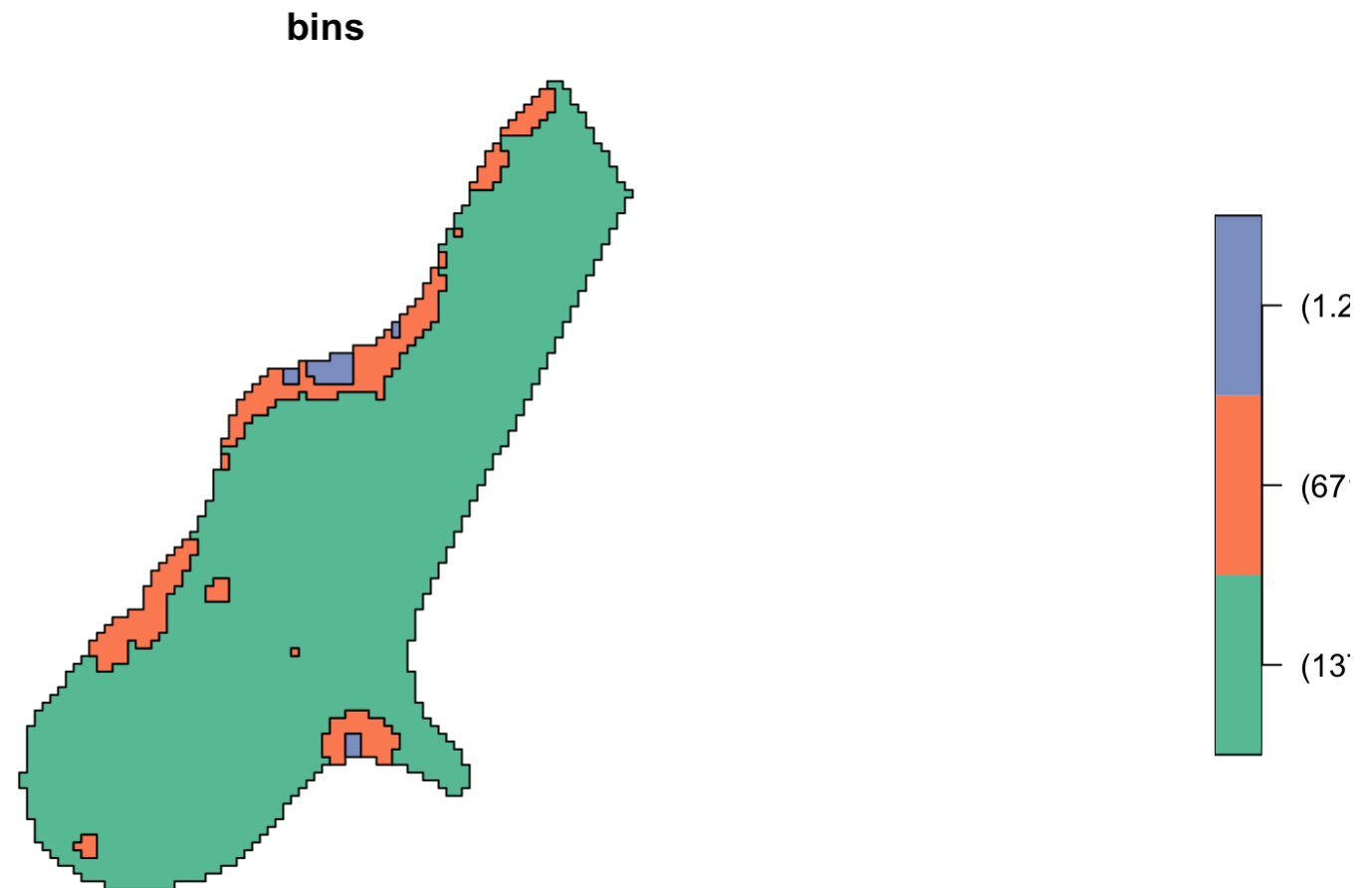
Polygonization

```
1 meuse_rast_poly = meuse_rast |>  
2   mutate(bins = cut(test.grd, 3) ) |>  
3   select(bins) |>  
4   st_as_sf()  
5 plot(meuse_rast_poly)
```

bins



```
1 meuse_rast_poly |>  
2   group_by(bins) |>  
3   summarize() |>  
4   plot()
```



```

1 meuse_rast_poly |>
2   group_by(bins) |>
3   summarize() |>
4   mutate(area = st_area(geometry))

```

Simple feature collection with 3 features and 2 fields

Geometry type: GEOMETRY

Dimension: XY

Bounding box: xmin: 178431 ymin: 329589.8 xmax: 181590.9 ymax: 333749.8

Projected CRS: Amersfoort / RD New

A tibble: 3 × 3

bins	geometry	area
* <fct>	<GEOMETRY [m]>	[m^2]
1 (137,671]	POLYGON ((178551 329829.8, 178511 329829.8, 17...	4.56e6
2 (671,1.2e+03]	MULTIPOLYGON (((178711 329829.8, 178751 329829...	4.74e5
3 (1.2e+03,1.74e+03]	MULTIPOLYGON (((179790.9 332189.8, 179790.9 33...	5.12e4

